

# Modified predictive torque and flux control for open end winding induction motor drive based on ranking method

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**Abstract:** The emerging application of predictive torque and flux control (PTC) in induction motor (IM) drive technology is becoming more successful. The PTC scheme can be applied to open-end winding IM (OEWIM) drive fed by dual inverter owing to its merits: high dynamic performance, simple control by involving regulation parameters into the control law. However, a conventional PTC offers single control law. To achieve controlling of multiple parameters, weighting factors need to be assigned to the respective parameters in the control law. The selection of weighting factors directly affects control performance of OEWIM. For an optimal selection of weighting factors, the empirical method has to be followed, which is time overwhelming and cumbersome process. To overcome this problem, this study introduces multi-objective controlling and optimisation based on the ranking method rather than the minimisation of single control law as in the case of conventional methods. The proposed feature circumvents optimisation of weighting factors. To validate the proposed scheme, simulation using Matlab/Simulink and experimental analysis are performed for dual-inverter fed OEWIM drive. By considering same control objectives (torque, flux ripple and switching frequency limitation), these results are examined with a conventional PTC scheme to accentuate merits of the proposed scheme.

## 1 Introduction

Variable speed induction motor (IM) drives fed by voltage source inverters (VSIs) became more popular for industrial applications. The current development is to use multilevel inverters (MLIs) for electric drive applications [1]. The increase in the number of voltage vectors means precise control, improvement of torque and flux regulation [1]. Apart from MLIs present in [2–4], the multilevel inversion with dual-inverter fed open-end winding IM (OEWIM) drive attains prominent status owing to its merits: simple structure, elimination of clamping diodes as related to the neutral point clamped (NPC) structure, requirement of fewer DC-link voltages compared to cascaded H-bridge inverter configuration. The several applications of OEWIM drive are documented in [5]. To improve the dynamic response of the drive, several control methods are introduced. The first innovation is started with field oriented control of IM drive in former 1960s [6–8]. The controlling is achieved in a rotating frame of reference. Requirement of current proportional–integral (PI) regulators, rotor flux observer and reference frame transformations hike computational complexity of the control scheme. To overcome these demerits, direct torque control (DTC) is hosted in the year 1986 [9]. It offers controlling in a stationary frame of reference and has a direct impact on torque control by applying appropriate voltage vector. The limitations of this scheme are the following: The inclusion of non-linear hysteresis controllers (flux and torque) demands high sampling frequency in a digital platform, large ripples in torque and flux, dependent of switching frequency on hysteresis band and motor speed. These limitations are addressed in [10–14].

Recently predictive control is introduced in control process [15]. It is applicable for both converter and electric drive applications [16–19]. Model predictive control (MPC) is the part of the predictive control and it is classified into two types. They are continuous control set MPC and finite control set MPC (FCS-PTC). FCS-PTC is gaining more importance and emerging technology in the field of electric drives. Its intuitive nature, simple control, direct involvement of control parameters, the absence of heuristic look-up tables and hysteresis controllers highlighted the advantages of PTC over the existing control schemes. In [20, 21],

PTC for the electric drive system is performed with an extended prediction horizon. In [22], PTC is performed on IM drive fed by three-phase four-switch inverter configuration. In [23], PTC is implemented on five-leg AC–DC–AC converter powered IM drive.

In predictive control, selection of optimal switching states for an inverter is based on depreciation of control law. Control law may involve different parameters (torque, flux, common mode voltage, switching frequency and reactive power) which have to be controlled [24–26]. The involvement of different control parameters in one control law necessitates the assignment of weighting factors to the respective terms. The weighting factor assignment creates relative balance among the various control terms and plays a key role in optimal control performance. Hence, its assignment in the control law became a major issue. With the involvement of additional control terms in control law, a number of weighting factors increases and its proper tuning becomes more complex.

In [26], empirical guidelines are indicated by Cortes *et al.*, to solve the weighting factor selection problem. However, it is not an optimal selection. It is only weighting factor approximation. Determining the weights empirically, the predictive control of IM is performed in [27–33]. The analytical method is exercised in [34] to accomplish an optimal weighting factor for a three-phase VSI fed IM. It is analysed with only torque and flux control objectives. Furthermore, it involves complex control and system parameter dependent. To achieve weights optimisation in [35], multi-objective genetic algorithm (GA)-based method is adopted. It necessitates a lot of search process prior to control. For IM drive control in [36, 37], multi-criteria-based VIKOR and TOPSIS methods are introduced. In this process, weighting factor coefficients are not altogether removed and analysed with only torque and flux control terms. In [38], fuzzy-based online tuning of weighting factors is implemented for four-leg VSI fed IM. In [39, 40] PTC scheme is performed on OEWIM drive. Here weighting factors are selected empirically in the cost function. The tuning of the weighting factors becomes effortful and time consuming with the increase of a number of objectives. In [41], PTC is performed on the indirect matrix converter fed IM where torque ripple reduction is achieved by weighting factor optimisation.

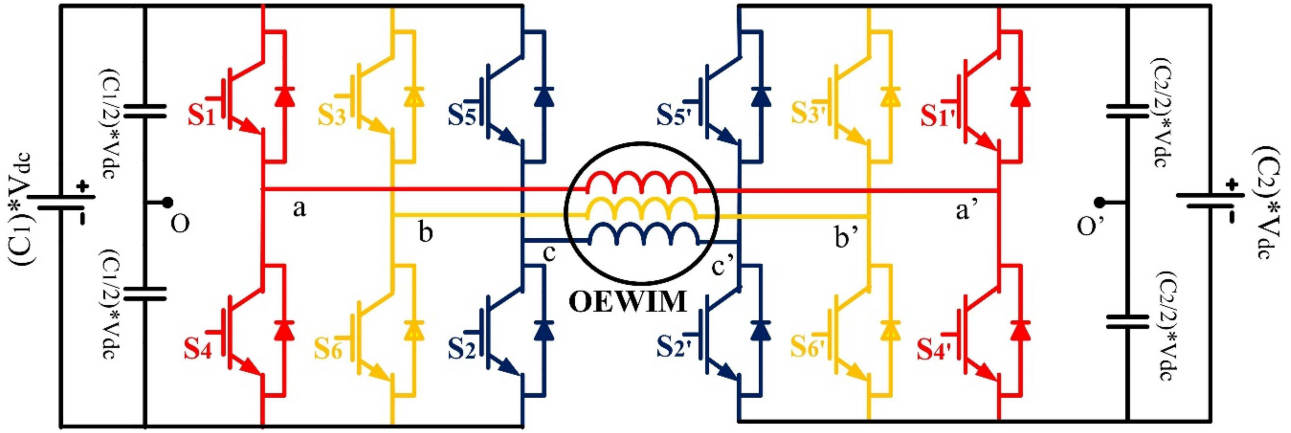


Fig. 1 OEWM power circuit

This paper presents a modified FCS-PTC, where single control law is replaced by multiple objectives. The optimisation of these multiple objectives is done by ranking analysis. This simple feature enables omission of weighting factors in PTC. The proposed scheme is applied for OEWM drive by considering three main objective functions (torque, flux control and switching frequency minimisation). The remaining part of the paper is organised as follows: Section 2 depicts the configuration of OEWM and its mathematical modelling. Detailed information about basic PTC is explained in Section 3. Section 4 introduces the new FCS-PTC scheme. Simulation and experimental results of the proposed PTC in comparison with conventional PTC are presented in Section 5. Finally, the conclusion is derived in Section 6.

## 2 OEWM configuration and mathematical modelling

Fig. 1 represents the power circuit of dual-inverter fed OEWM. In order to achieve multi-level inversion, DC-link voltages of the dual inverter (VSI-1 and VSI-2) should be in the ratio of 2:1. Therefore, DC-link voltage of VSI-1 is maintained to  $2V_{dc}/3$  and for VSI-2 it is maintained to  $V_{dc}/3$ . VSI-1 and VSI-2 pole voltages are represented by (1) and (2). From these, phase voltages are represented as (6). These phase voltages are applied to IM phases as shown in Fig. 1

$$\begin{pmatrix} V_{ao} \\ V_{bo} \\ V_{co} \end{pmatrix} = (C_1 V_{dc}) \times \begin{pmatrix} S_a \\ S_b \\ S_c \end{pmatrix} \quad (1)$$

$$\begin{pmatrix} V_{a'o'} \\ V_{b'o'} \\ V_{c'o'} \end{pmatrix} = (C_2 V_{dc}) \times \begin{pmatrix} S_{a'} \\ S_{b'} \\ S_{c'} \end{pmatrix} \quad (2)$$

where  $C_1$  and  $C_2$  are constants which are given as

$$C_1 = \frac{2}{3}, \quad C_2 = \frac{1}{3} \quad (3)$$

$$\begin{pmatrix} \Delta V_{aa'} \\ \Delta V_{bb'} \\ \Delta V_{cc'} \end{pmatrix} = \begin{pmatrix} V_{ao} - V_{a'o'} \\ V_{bo} - V_{b'o'} \\ V_{co} - V_{c'o'} \end{pmatrix}$$

The sum of pole voltage differences ( $\Delta V_{aa'}$ ,  $\Delta V_{bb'}$  and  $\Delta V_{cc'}$ ) is not equal to zero. This indicates the presence of zero sequence voltage [5] which is given as

$$V_z = \frac{1}{3} \times (\Delta V_{aa'} + \Delta V_{bb'} + \Delta V_{cc'}) \quad (4)$$

The phase voltages are given as

$$\begin{pmatrix} V_{aa'} \\ V_{bb'} \\ V_{cc'} \end{pmatrix} = \begin{pmatrix} \Delta V_{aa'} \\ \Delta V_{bb'} \\ \Delta V_{cc'} \end{pmatrix} - \begin{pmatrix} V_z \\ V_z \\ V_z \end{pmatrix} \quad (5)$$

By substitution of (4) into (5), the phase voltages are obtained in terms of pole voltages as

$$\begin{pmatrix} V_{aa'} \\ V_{bb'} \\ V_{cc'} \end{pmatrix} = \frac{1}{3} \begin{pmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{pmatrix} \times \begin{pmatrix} \Delta V_{aa'} \\ \Delta V_{bb'} \\ \Delta V_{cc'} \end{pmatrix} \quad (6)$$

The OEWM is modelled in stationary reference frame [42]. The machine stator and rotor voltages are represented as (7) and (8). Stator and rotor flux linkages are given as (9) and (10). Electromechanical conversion is represented by (11) and (12)

$$\begin{pmatrix} V_{sa} \\ V_{s\beta} \end{pmatrix} = R_s \begin{pmatrix} i_{sa} \\ i_{s\beta} \end{pmatrix} + p \begin{pmatrix} \lambda_{sa} \\ \lambda_{s\beta} \end{pmatrix} \quad (7)$$

$$\begin{pmatrix} 0 \\ 0 \end{pmatrix} = R_r \begin{pmatrix} i_{ra} \\ i_{r\beta} \end{pmatrix} + p \begin{pmatrix} \lambda_{ra} \\ \lambda_{r\beta} \end{pmatrix} + \omega_r \begin{pmatrix} \lambda_{r\beta} \\ -\lambda_{ra} \end{pmatrix} \quad (8)$$

$$\begin{pmatrix} \lambda_{sa} \\ \lambda_{s\beta} \end{pmatrix} = L_s \begin{pmatrix} i_{sa} \\ i_{s\beta} \end{pmatrix} + L_m \begin{pmatrix} i_{ra} \\ i_{r\beta} \end{pmatrix} \quad (9)$$

$$\begin{pmatrix} \lambda_{ra} \\ \lambda_{r\beta} \end{pmatrix} = L_r \begin{pmatrix} i_{ra} \\ i_{r\beta} \end{pmatrix} + L_m \begin{pmatrix} i_{sa} \\ i_{s\beta} \end{pmatrix} \quad (10)$$

$$T_{motor} = \left( \frac{3}{2} \right) \left( \frac{P}{2} \right) (\lambda_{sa} i_{s\beta} - \lambda_{s\beta} i_{sa}) \quad (11)$$

$$J \frac{d\omega_m}{dt} = T_{motor} - T_{load} \quad (12)$$

where subscript 's' and 'r' represents stator and rotor terms, respectively,  $p = d/dt$ ,  $J$  is the moment of inertia and  $\omega_m$  is the mechanical speed of the motor.

The state-space representation of these (7)–(10) considering a space vector  $i_s$  and  $\lambda_s$  as state variables are shown as

$$\frac{di_s}{dt} = S_1 \left( S_2 \lambda_s - S_3 i_s + K_r (V_s - S_i i_s - j\omega_r \lambda_s) + \frac{j\omega_r i_s}{S_1} \right) \quad (13)$$

$$\frac{d\lambda_s}{dt} = (V_s - S_i i_s) \quad (14)$$

where

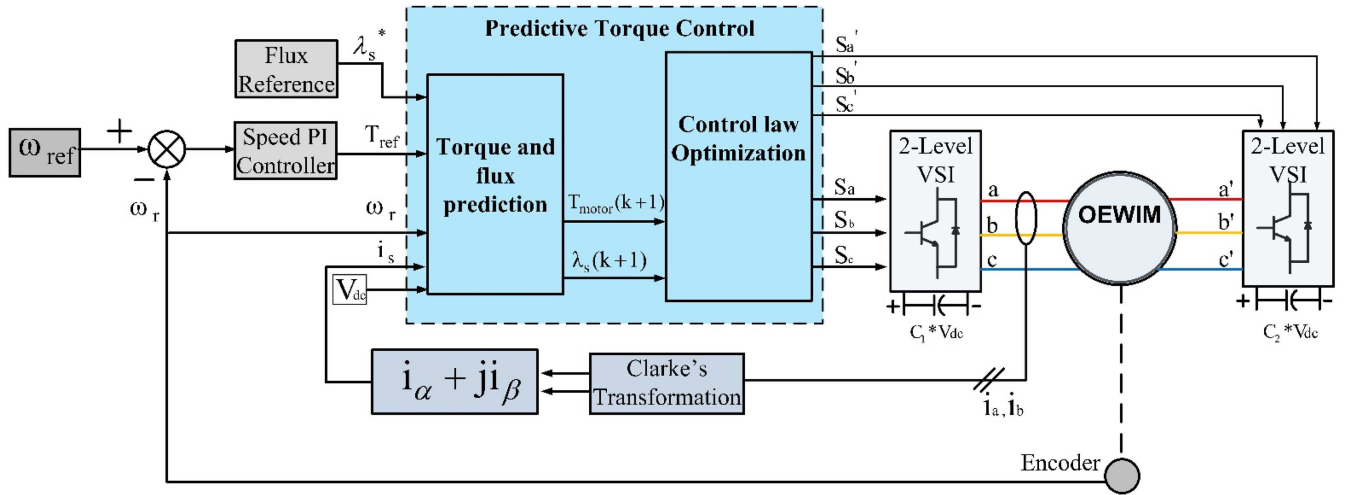


Fig. 2 Basic PTC block diagram

$$\left. \begin{aligned} S &= R_s, S_1 = \frac{L_m}{L_s L_r - L_m^2}, S_2 = \frac{R_r}{L_m}, S_3 = \frac{L_s R_r}{L_m} \\ K_r &= \frac{L_r}{L_m}, i_s = i_{s\alpha} + j i_{s\beta}, \lambda_s = \lambda_{s\alpha} + j \lambda_{s\beta}, \\ V_s &= V_{s\alpha} + j V_{s\beta} \end{aligned} \right\} \quad (15)$$

In PTC algorithm these (13) and (14) are expressed in a discrete manner.

### 3 Basic PTC

The basic PTC functional block diagram is presented in Fig. 2. Speed PI controller generates torque reference. The input requirements to the PTC algorithm for controlling and realisation of switching states are motor speed, torque reference, flux reference, combined DC-link voltages and measured current. The discretisation of system mathematical model in PTC algorithm uses forward Euler's method. The standard illustration of it is shown as

$$\frac{dx}{dt} = \frac{x(k+1) - x(k)}{T_s} \quad (16)$$

where 'x' is any state variable, 'k' is the present sampling state and 'T<sub>s</sub>' is the sample time.

#### 3.1 Measurement and estimation

Direct measurement of machine stator flux is not possible. Due to this, Euler's method is used to estimate the present state stator flux as [42]

$$\lambda_s(k) = \lambda_s(k-1) + T_s((V_s(k-1)) - S i_s(k-1)) \quad (17)$$

The measured currents  $i_a, i_b$  and  $i_c$  from machine stator terminals undergoes Clarke's transformation, resulting to  $i_\alpha$  and  $i_\beta$  terms. From this, current space vector is represented.

#### 3.2 Prediction

The machine current, stator flux and torque are needed to predict for all the accessible switching states. For dual-inverter fed OEWM, there are 64 ( $8 \times 8$ ) possible switching combinations. Out of these, it offers 37 effective switching combinations. The voltage space-vector representation for VSI-I and VSI-2 are given as (18) and (19). The effective voltage space vector applied to the machine is formulated as (20)

$$V_{s1} = \left(\frac{2}{3}\right)(C_1 \times V_{dc})(S_a + S_b e^{j(2\pi/3)} + S_c e^{j(4\pi/3)}) \quad (18)$$

$$V_{s2} = \left(\frac{2}{3}\right)(C_2 \times V_{dc})(S_{a'} + S_{b'} e^{j(2\pi/3)} + S_{c'} e^{j(4\pi/3)}) \quad (19)$$

$$V_s = V_{s1} - V_{s2} \quad (20)$$

Table 1 denotes possible effective inverter switching states and its corresponding phase voltages in a stationary reference frame. For these switching states, space vector locations are presented in Fig. 3. One step ahead predicted flux, current and torque are characterised as [42]

$$\lambda_s(k+1)_n = \lambda_s(k) + T_s((V_s(k))_n - S i_s(k)) \quad (21)$$

$$i_s(k+1)_n = i_s(k) + T_s \left( S_1 \left( S_2 \lambda_s(k) - S_3 i_s(k) \right) + K_r((V_s(k))_n - S i_s(k) - j \omega_r \lambda_s(k)) + \frac{j \omega_r i_s(k)}{S_1} \right) \quad (22)$$

$$(T_{motor}(k+1))_n = \frac{3}{2} \frac{P}{2} (\text{imag}(\tilde{\lambda}_s(k+1) \times i_s(k+1)_n)) \quad (23)$$

where  $n = (V_0, V_1, V_2, \dots, V_{36})$ .

Thus, from (21)–(23), stator flux, current and torque are predicted for one step ahead with the 37 voltage vectors.

#### 3.3 Control law formulation

Basic PTC constitutes single control law [28]. Control law for torque and flux control is shown as

$$G_n = |T_{motor}^* - T_{motor}(k+1)_n| + W |\lambda_s^* - \lambda_s(k+1)_n| \quad (24)$$

where  $T_{motor}^*$  and  $\lambda_s^*$  are the reference motor torque and flux values, respectively.

This control law value is checked for every possible voltage vector. Among all the possibilities, voltage vector which provides the minimum value of control law is selected as optimal and its corresponding switching states are given to inverter switches. From (24), it can be observed that  $W$  (weighting factor) is the only adjustable term. Therefore, optimal voltage vector selection is affected by the relative importance of torque and flux. With the involvement of more number of control parameters, the complexity of weight factor assignment (to provide relative importance to them) increases. This has a direct influence on voltage vector selection. In [26–41], analytical and empirical methods are employed for proper tuning of weight factor which results in complex control.

**Table 1** Switching states and voltage vector realisation for dual-inverter fed OEWM

Space vector ( $V_s$ )	VSI-1 ( $S_a, S_b, S_c$ )	VSI-2 ( $S_a', S_b', S_c'$ )	Realisation	
			$V_\alpha$	$V_\beta$
$V_0$	(0, 0, 0)	(0, 0, 0)	0	0
$V_1$	(1, 0, 0)	(1, 0, 0)	$V_{dc}$ (0.222)	0
$V_2$	(1, 1, 0)	(1, 1, 0)	$V_{dc}$ (0.11)	(0.193) $V_{dc}$
$V_3$	(0, 1, 0)	(0, 1, 0)	$V_{dc}$ (-0.11)	(0.193) $V_{dc}$
$V_4$	(0, 1, 1)	(0, 1, 1)	$V_{dc}$ (-0.222)	0
$V_5$	(0, 0, 1)	(0, 0, 1)	$V_{dc}$ (-0.11)	(-0.193) $V_{dc}$
$V_6$	(1, 0, 1)	(1, 0, 1)	$V_{dc}$ (0.11)	(-0.193) $V_{dc}$
$V_7$	(1, 0, 0)	(1, 1, 1)	$V_{dc}$ (0.444)	0
$V_8$	(1, 0, 0)	(1, 0, 1)	$V_{dc}$ (0.33)	(0.193) $V_{dc}$
$V_9$	(1, 1, 0)	(1, 1, 1)	$V_{dc}$ (0.222)	(0.385) $V_{dc}$
$V_{10}$	(0, 1, 0)	(0, 1, 1)	0	(0.385) $V_{dc}$
$V_{11}$	(0, 1, 0)	(1, 1, 1)	$V_{dc}$ (-0.222)	(0.385) $V_{dc}$
$V_{12}$	(0, 1, 0)	(1, 1, 0)	$V_{dc}$ (-0.33)	(0.193) $V_{dc}$
$V_{13}$	(0, 1, 1)	(1, 1, 1)	$V_{dc}$ (-0.444)	0
$V_{14}$	(0, 0, 1)	(1, 0, 1)	$V_{dc}$ (-0.33)	(-0.193) $V_{dc}$
$V_{15}$	(0, 0, 1)	(1, 1, 1)	$V_{dc}$ (-0.222)	(-0.385) $V_{dc}$
$V_{16}$	(0, 0, 1)	(0, 1, 1)	0	(-0.385) $V_{dc}$
$V_{17}$	(1, 0, 1)	(1, 1, 1)	$V_{dc}$ (0.222)	(-0.385) $V_{dc}$
$V_{18}$	(1, 0, 0)	(1, 1, 0)	$V_{dc}$ (0.33)	(-0.193) $V_{dc}$
$V_{19}$	(1, 0, 0)	(0, 1, 1)	$V_{dc}$ (0.667)	0
$V_{20}$	(1, 0, 0)	(0, 0, 1)	$V_{dc}$ (0.55)	(0.193) $V_{dc}$
$V_{21}$	(1, 1, 0)	(0, 1, 1)	$V_{dc}$ (0.44)	(0.385) $V_{dc}$
$V_{22}$	(1, 1, 0)	(0, 0, 1)	$V_{dc}$ (0.33)	(0.577) $V_{dc}$
$V_{23}$	(1, 1, 0)	(1, 0, 1)	$V_{dc}$ (0.11)	(0.577) $V_{dc}$
$V_{24}$	(0, 1, 0)	(0, 0, 1)	$V_{dc}$ (-0.11)	(0.577) $V_{dc}$
$V_{25}$	(0, 1, 0)	(1, 0, 1)	$V_{dc}$ (-0.33)	(0.577) $V_{dc}$
$V_{26}$	(0, 1, 0)	(1, 0, 0)	$V_{dc}$ (-0.44)	(0.385) $V_{dc}$
$V_{27}$	(0, 1, 1)	(1, 0, 1)	$V_{dc}$ (-0.55)	(0.193) $V_{dc}$
$V_{28}$	(0, 1, 1)	(1, 0, 0)	$V_{dc}$ (-0.667)	0
$V_{29}$	(0, 1, 1)	(1, 1, 0)	$V_{dc}$ (-0.55)	(-0.193) $V_{dc}$
$V_{30}$	(0, 0, 1)	(1, 0, 0)	$V_{dc}$ (-0.44)	(-0.385) $V_{dc}$
$V_{31}$	(0, 0, 1)	(1, 1, 0)	$V_{dc}$ (-0.33)	(-0.577) $V_{dc}$
$V_{32}$	(0, 0, 1)	(0, 1, 0)	$V_{dc}$ (-0.11)	(-0.577) $V_{dc}$
$V_{33}$	(1, 0, 1)	(1, 1, 0)	$V_{dc}$ (0.11)	(-0.577) $V_{dc}$
$V_{34}$	(1, 0, 1)	(0, 1, 0)	$V_{dc}$ (0.33)	(-0.577) $V_{dc}$
$V_{35}$	(1, 0, 1)	(0, 1, 1)	$V_{dc}$ (0.44)	(-0.385) $V_{dc}$
$V_{36}$	(1, 0, 0)	(0, 1, 0)	$V_{dc}$ (0.55)	(-0.193) $V_{dc}$

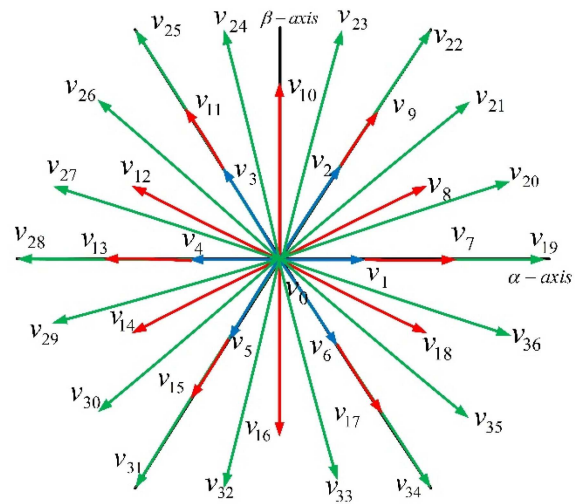
## 4 Proposed PTC

It is established that the following are the most prime steps involved in PTC: (i) estimation of unknowns which are not measurable, (ii) system behaviour prediction and (iii) control law minimisation. Due to the key issues faced by basic PTC, this paper proposed a ranking based multi-objective optimisation. It relieves PTC from weighting factor tuning. Fig. 4 depicts the pictorial representation of the proposed control algorithm.

Execution steps for the ranking method are given as follows:

### 4.1 Step 1: separation of multi objectives

Torque and stator flux are considered as separate objectives ( $G_1$  and  $G_2$ ). Because of the presence of two VSI bridges (increase in the number of switches), switching frequency is to be limited to minimise overall switching losses in OEWM drive. This limitation can be easily achieved by considering one more objective ( $G_3$ ), which reduces state voltage variations. With this, voltage vector



**Fig. 3** Space vector allocations

remains to be the same for some sample duration and has a direct impact on switching frequency reduction. Therefore multi-objective ( $G_1$ ,  $G_2$  and  $G_3$ ) are represented as

$$(G_1)_n = |T_{\text{motor}}^* - T_{\text{motor}}(k+1)_n| \quad (25)$$

$$(G_2)_n = |\lambda_s^* - \lambda_s(k+1)_n| \quad (26)$$

$$(G_3)_n = |V_s(k-1) - V_s(k)_n| \quad (27)$$

The above objectives (25)–(27) are formulated with one step ahead. With this, there exist practical sample delay problems which can affect control performance. To circumvent this problem, two-step ahead prediction is preferred. The modified multi-objectives are represented as

$$(G_1)_n = |T_{\text{motor}}^* - T_{\text{motor}}(k+2)_n| \quad (28)$$

$$(G_2)_n = |\lambda_s^* - \lambda_s(k+2)_n| \quad (29)$$

$$(G_3)_n = |V_s(k) - V_s(k+1)_n| \quad (30)$$

where

$$(\lambda_s(k+2))_n = \lambda_s(k+1) + T_s((V_s(k+1))_n - S_{i_s}(k+1)) \quad (31)$$

$$i_s(k+2)_n = i_s(k+1) + T_s \left( S_1 \left( \begin{aligned} &S_2 \lambda_s(k+1) - S_3 i_s(k+1) \\ &+ K_r \left( (V_s(k+1))_n - S_{i_s}(k+1) \right) \\ &- j\omega_r \lambda_s(k+1) \\ &+ \frac{j\omega_r i_s(k+1)}{S_1} \end{aligned} \right) \right) \quad (32)$$

$$(T_{\text{motor}}(k+2))_n = \frac{3P}{2} (\text{imag}(\bar{\lambda}_s(k+2)_n \times i_s(k+2)_n)) \quad (33)$$

### 4.2 Step 2: evaluation and ranking

The multi-objectives (torque (28), flux (29) and switching state variation (30) errors) are evaluated for all the available 37 voltage vectors and rankings ( $R_1$ ,  $R_2$  and  $R_3$ ) are assigned corresponding to their values. The value with minimum error assigned lower rank-0 and from this point with increase in error, ranking value also increases.

### 4.3 Step 3: optimal selection

Each voltage vector constitutes different rankings based on error values of multi-objectives. For a given voltage vector, all the obtained rankings are averaged. The voltage vector (VV) achieving



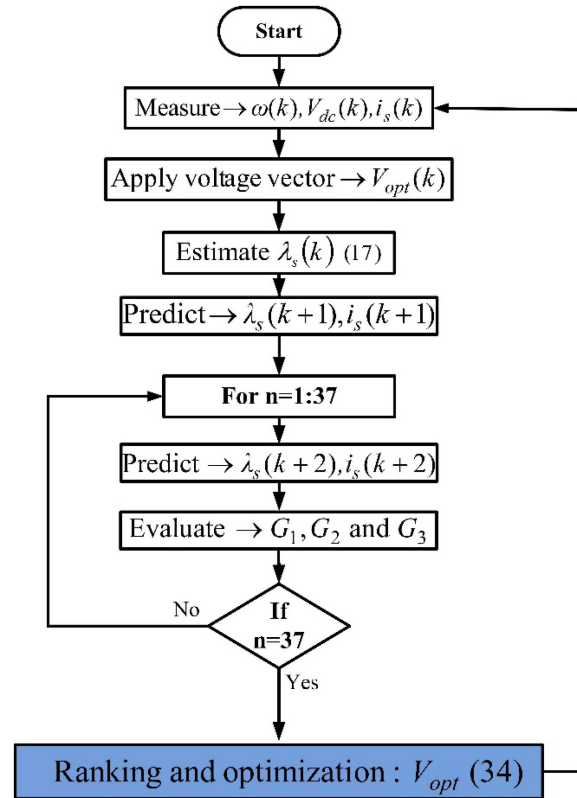


Fig. 4 Proposed PTC flowchart

minimum averaged rank value is selected as optimal for the next sampling period. It is represented as

$$V_{opt} = VV \left[ \min \left( \frac{R_1 + R_2 + R_3}{3} \right) \right] \quad (34)$$

The control algorithm is demonstrated for one sampling period. Multi-objective rankings for all the switching states and selection of optimal switching state are represented in Table 2. In this sampling period, voltage vector  $V_9$  offers minimum averaged rank among the all, which is considered as optimal and corresponding switching states are given to dual inverter switches. This control process is completely independent of weighting factor assignment. Thereby, achieving optimal control response for OEWM drive.

## 5 Results and discussion

The simulations and real-time experimentation are performed for both conventional and proposed PTC schemes of OEWM drive. The experimental setup is presented in Fig. 5.

### 5.1 Simulation results

To validate the proposed control strategy as presented in Section 4, simulation and experimentation are performed on dual-inverter fed OEWM. Machine modelling is carried out using mathematical (1)–(12) and simulations are executed in Matlab/Simulink environment. The existing machine specifications are presented in Table 3 which are considered for simulation analysis. DC-link voltages of VSI-1 and VSI-2 are set to 333.33 and 166.67 V, respectively, with a combined voltage of 500 V ( $V_{dc}$ ). The reference value of stator flux is set to 1 Wb (nominal). Both simulation and experiment are run at no load with a sampling time of 100  $\mu$ s. To study the proposed PTC effectiveness with respect to conventional, conventional weighting factors are designated in basic PTC control law as stated by

$$G_n = |T_{motor}^* - T_{motor}(k+2)_n| + W_1 |\lambda_s^* - \lambda_s(k+2)_n| + W_2 |V_s(k) - V_s(k+1)_n| \quad (35)$$

where  $W_1$  and  $W_2$  are flux and switching frequency weighting factors, respectively.

The flux weighting factor ( $W_1$ ) selection for conventional PTC is considered from [28, 40], where the ratio of nominal torque and flux value ( $T_{nom}/\lambda_{nom}$ ) is considered at starting. Later, this value is adjusted empirically to attain better performance, which is time consuming. Thus, these values are empirically set as  $W_1 = 75$  and  $W_2 = 0.001$ . These are only approximated values.

The results of OEWM drive are represented in Figs. 6–11. At starting, steady-state behaviour of the machine is analysed. For the reference electrical speed of 250 rad/s, the simulated response of motor speed, current and phase voltage are shown in Figs. 6a and c. From these simulated results, it is observed that the proposed PTC is exhibiting optimal speed and current response, compared to the basic PTC. For the reference speeds of 100 and 250 rad/s (low and high), the simulated response of motor speed, torque and flux are shown in Figs. 7a–d top. From these results, optimal torque and flux response are observed in the proposed PTC, exhibiting reduced torque and flux ripples compared to the basic PTC.

To analyse machine dynamics, step changes in reference speed are performed from 150 to 200 rad/s and then 200 to 250 rad/s. The simulated dynamic response of motor speed, torque and flux are shown in Figs. 8a and c. These results convey forward motoring. The same can be analysed with reverse motoring by feeding reference step changes in the reverse direction, i.e. from –150 to –200 rad/s and then –200 to –250 rad/s. Its simulated motor speed, torque and flux characteristics are shown in Figs. 9a and c.

Finally, when the motor is operating at 200 rad/s, a step change is triggered from 200 to –200 rad/s which conveys speed reversal. The simulated characteristics (motor speed, torque and flux) are shown in Figs. 10a and c. From the simulation results, it is observed that the proposed PTC exhibits optimal control performance without making any effort of weighting factor selection.

### 5.2 Experimental results

For real-time execution, the proposed PTC is tested on 3.7 kW, 1440 RPM OEWM drive fed by two, two-level VSIs. The interface dSPACE (RTI 1104) setup is used to execute the proposed

**Table 2** Control performance in one sample interval

Voltage space vector ( $V_s$ )	$G_1$	$G_2$	$G_3$	$R_1$	$R_2$	$R_3$	$\frac{1}{3} \times (R_1 + R_2 + R_3)$
$V_0$	2.5908	0.0023	192.4501	18	2	2	7.333333
$V_1$	1.6611	0.0105	111.1111	13	13	1	9
$V_2$	1.2221	0.0001	111.1111	10	0	1	3.666667
$V_3$	2.1517	0.0083	222.2222	16	11	3	10
$V_4$	3.5205	0.0058	293.9724	23	7	4	11.333333
$V_5$	3.9595	0.0048	293.9724	25	6	4	11.666667
$V_6$	3.0299	0.0129	222.2222	20	16	3	13
$V_7$	0.7315	0.0187	111.1111	6	23	1	10
$V_8$	0.2924	0.0081	0	2	10	0	4
<b><math>V_9</math></b>	<b>0.1466</b>	<b>0.0024</b>	<b>111.1111</b>	<b>0</b>	<b>3</b>	<b>1</b>	<b>1.333333</b>
$V_{10}$	0.783	0.0107	192.4501	7	14	2	7.666667
$V_{11}$	1.7127	0.0189	293.9724	14	24	4	14
$V_{12}$	3.0814	0.0164	333.3333	21	21	5	15.666667
$V_{13}$	4.4501	0.0139	400.6168	28	18	7	17.666667
$V_{14}$	4.8892	0.0032	384.9002	30	4	6	13.333333
$V_{15}$	5.3283	0.0075	400.6168	31	9	7	15.666667
$V_{16}$	4.3986	0.0155	333.3333	27	19	5	17
$V_{17}$	3.4689	0.0236	293.9724	22	28	4	18
$V_{18}$	2.1002	0.0211	192.4501	15	25	2	14
$V_{19}$	0.1982	0.027	192.4501	1	31	2	11.333333
$V_{20}$	0.6372	0.0164	111.1111	5	20	1	8.666667
$V_{21}$	1.0763	0.0059	111.1111	8	8	1	5.666667
$V_{22}$	1.5154	0.0046	192.4501	12	5	2	6.333333
$V_{23}$	0.5857	0.013	222.2222	4	17	3	8
$V_{24}$	0.3439	0.0213	293.9724	3	26	4	11
$V_{25}$	1.2736	0.0295	384.9002	11	34	6	17
$V_{26}$	2.6423	0.0271	400.6168	19	32	7	19.333333
$V_{27}$	4.0111	0.0245	444.4444	26	29	8	21
$V_{28}$	5.3798	0.0219	509.1751	32	27	10	23
$V_{29}$	5.8188	0.0112	484.3221	34	15	9	19.333333
$V_{30}$	6.2579	0.0005	484.3221	35	1	9	15
$V_{31}$	6.697	0.0103	509.1751	36	12	10	19.333333
$V_{32}$	5.7673	0.0182	444.4444	33	22	8	21
$V_{33}$	4.8377	0.0262	400.6168	29	30	7	22
$V_{34}$	3.908	0.0342	384.9002	24	36	6	22
$V_{35}$	2.5393	0.0317	293.9724	17	35	4	18.666667
$V_{36}$	1.1705	0.0293	222.2222	9	33	3	15

Bold values represent optimal voltage space vector achieved with the proposed PTC strategy.

algorithm in the discrete platform. The machine parameters are mentioned in Table 3. DC-link voltages are measured using voltage sensors (LV-25). Stator phase currents are measured using two currents sensors (LA-25). From the encoder, motor speed is measured and connected to the dSPACE Incremental Encoder. All these sensed variables are given to control algorithm by ADC BNC connectors. The controlled switching pulses are acquired from dSPACE controller board and interfaced to dual inverter switches using the digital I/O connector.

The steady-state experimental results of motor speed, phase current and voltage for the reference speed 250 rad/s are represented in Figs. 6*b* and *d*. From these, optimal steady-state speed and current characteristics are achieved with the proposed PTC scheme compared to the basic PTC. From the experimental voltage waveforms as shown in Figs. 6*b* and *d*, minimal voltage state transitions are observed in the proposed PTC. The steady-state motor speed, estimated torque and flux response for the reference speeds 100 and 250 rad/s are shown in Figs. 7*a–d* bottom. From these, it is evident that the maximum flux and torque

ripple are less in the proposed PTC compared to the basic PTC. For testing dynamic conditions, motor reference speed is varied online from dSPACE control desk software. A step change in reference speed is assigned from 150 to 200 and 200 to 250 rad/s. Its corresponding motor speed, torque and flux response are shown in Figs. 8*b* and *d*. These characteristics signify the forward motoring operation.

For reverse motoring operation, reference speed step changes are considered from –150 to –200 rad/s and –200 to –250 rad/s. The motor speed, torque and flux characteristics are shown in Figs. 9*b* and *d*.

For speed reversal operation, reference speed step changes are considered from 200 to –200 rad/s (forward to reverse motoring). Figs. 10*b* and *d* represent the motor speed, torque and flux dynamic characteristics during speed reversal operation. From the performed dynamic analysis, it is observed that both control schemes provide similar characteristics with reduced steady state ripples. The switching transitions from the available 37 voltage vectors for both basic and proposed PTC at speed 200 rad/s are

represented in Figs. 11*a* and *b*. From Fig. 11*b*, minimal switching transitions are observed in the proposed PTC scheme. From the

observed experimental results, a comparative tabular structure is prepared as shown in Table 4 to compare maximum torque, flux

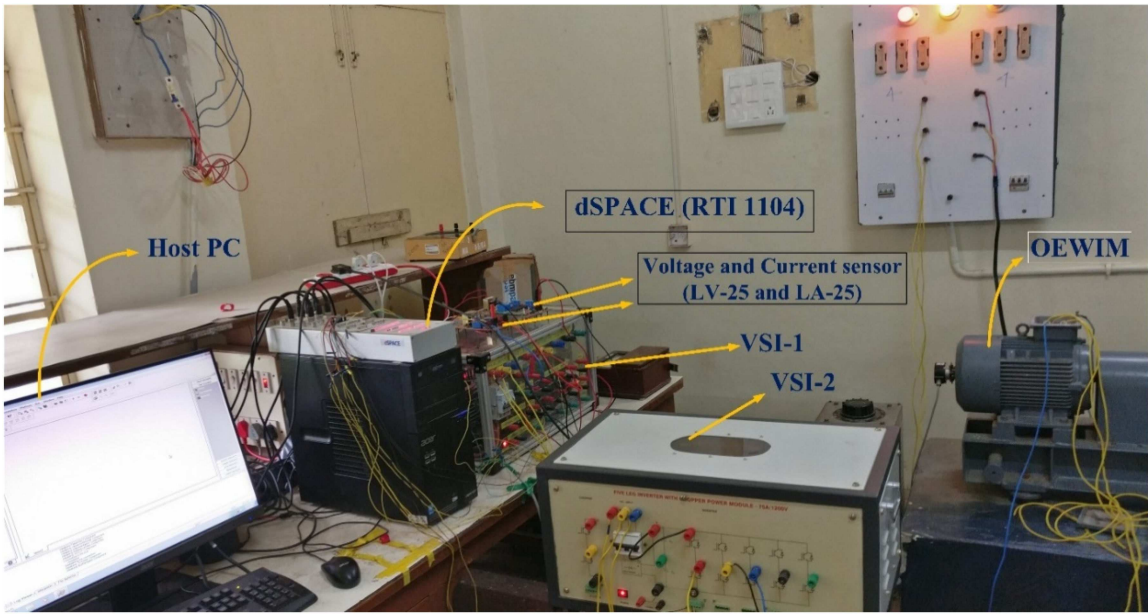


Fig. 5 Experimental test rig of OEWIM drive

Table 3 Machine specifications

Parameter	Quantity
stator resistance ( $R_s$ )	4.2 $\Omega$
rotor resistance ( $R_r$ )	2.6794 $\Omega$
stator inductance ( $L_s$ )	0.54 H
rotor inductance ( $L_r$ )	0.54 H
mutual inductance ( $L_m$ )	0.512 H
poles ( $P$ )	4
inertia ( $J$ )	0.031 kg/m <sup>2</sup>
motor nominal voltage	415 V (line-line)

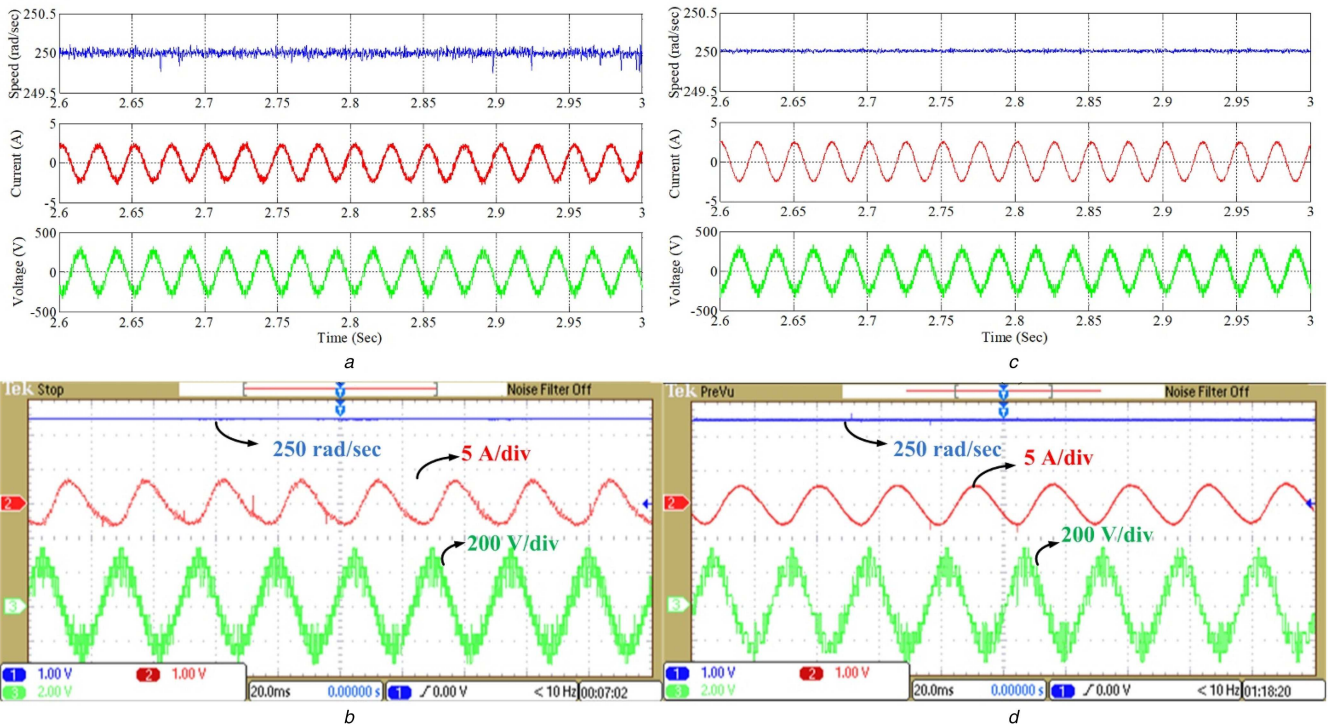
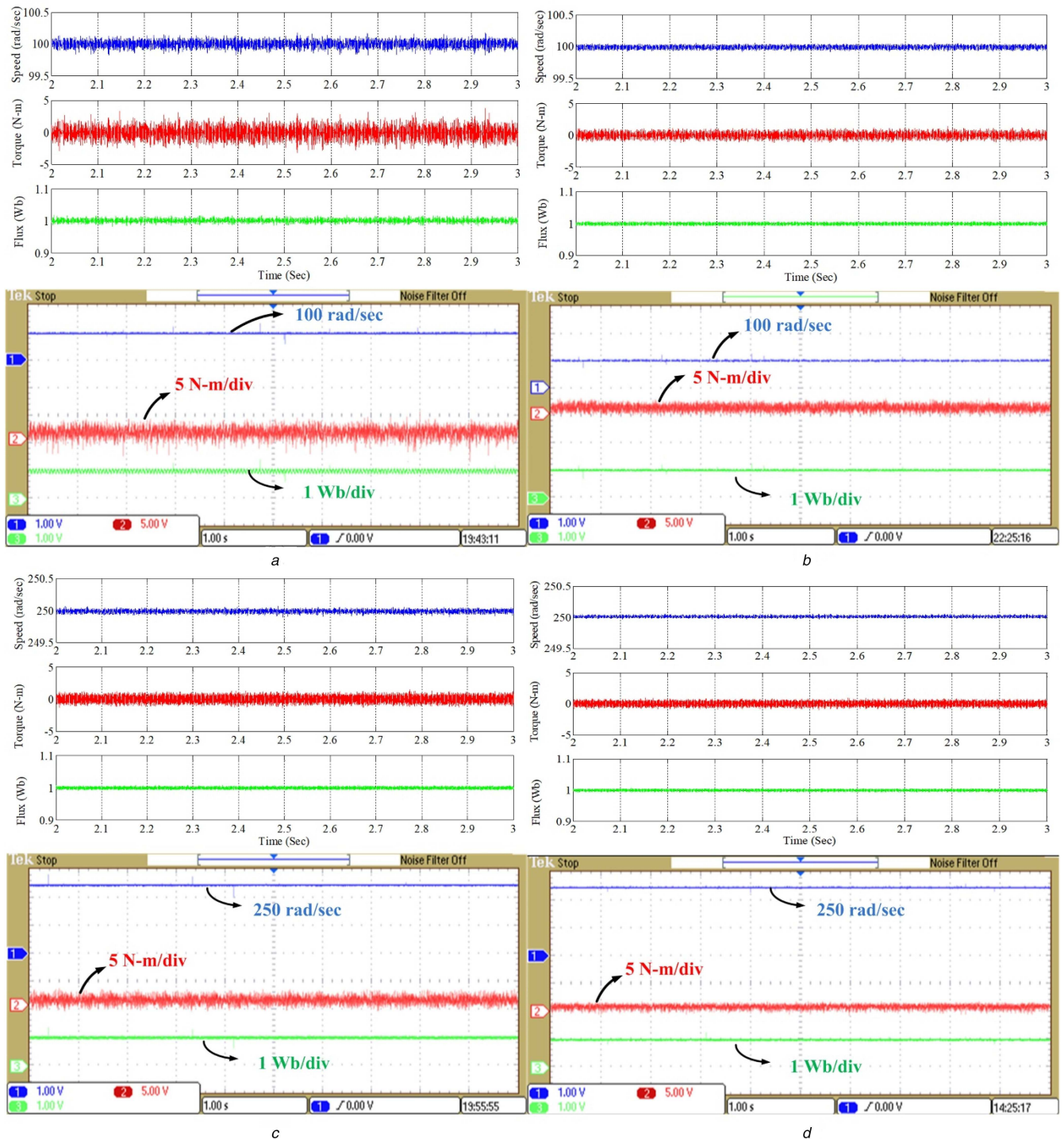


Fig. 6 Steady-state response of motor speed, current and voltage at 250 rad/s  
(a) Basic PTC simulation, (b) Basic PTC experimental results, (c) Proposed PTC simulation, (d) Proposed PTC experimental results





**Fig. 7** Motor speed, torque and flux steady-state characteristics at 100 and 250 rad/s

(a) Basic PTC simulation and experimental results at 100 rad/s, (b) Proposed PTC simulation and experimental results at 100 rad/s, (c) Basic PTC simulation and experimental results at 250 rad/s, (d) Proposed PTC simulation and experimental results at 250 rad/s

ripples and the average switching frequency of the proposed PTC with the existing control scheme at different operating speeds (100, 150 and 250 rad/s). From these results Figs. 7–11, torque and flux response for the proposed PTC is improved with reduced steady-state ripples compared to the conventional scheme. Switching frequency also minimised compared to a basic control scheme as shown in Fig. 12. This validates optimal control response and effortless control of the proposed PTC over the conventional scheme.

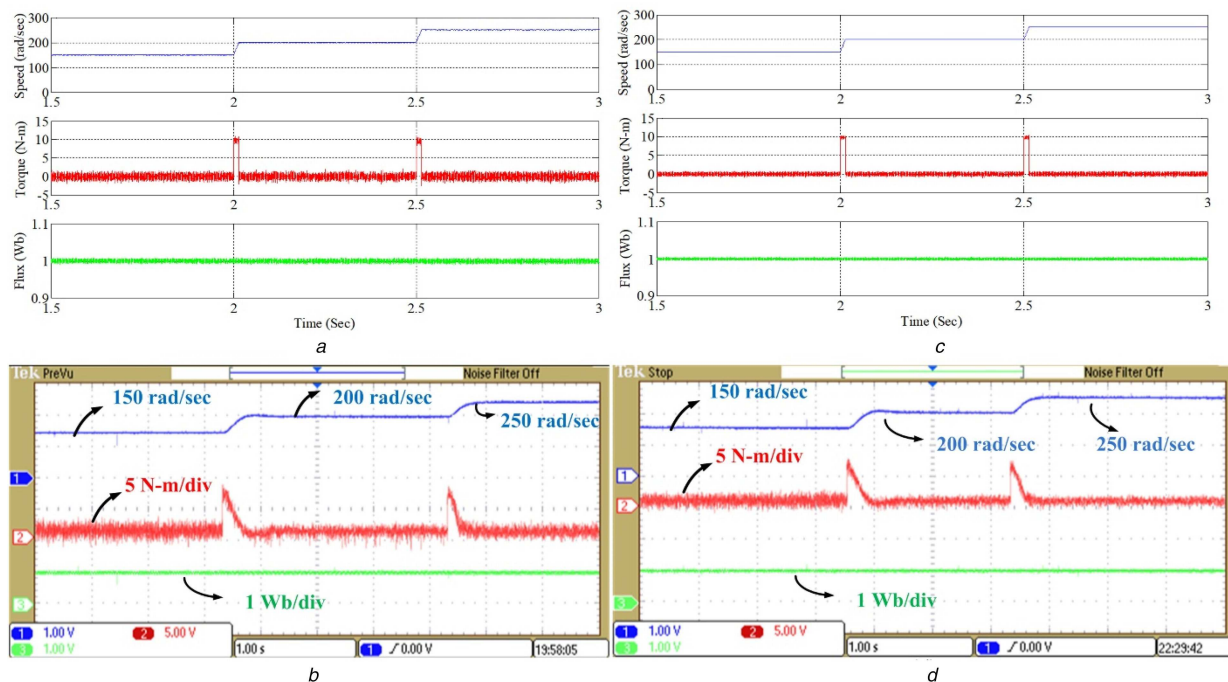
## 6 Conclusion

In basic PTC, the weighting factor selection in single control law and its tuning determines optimal control response. This is only troublesome and time consuming. This paper proposed a simple

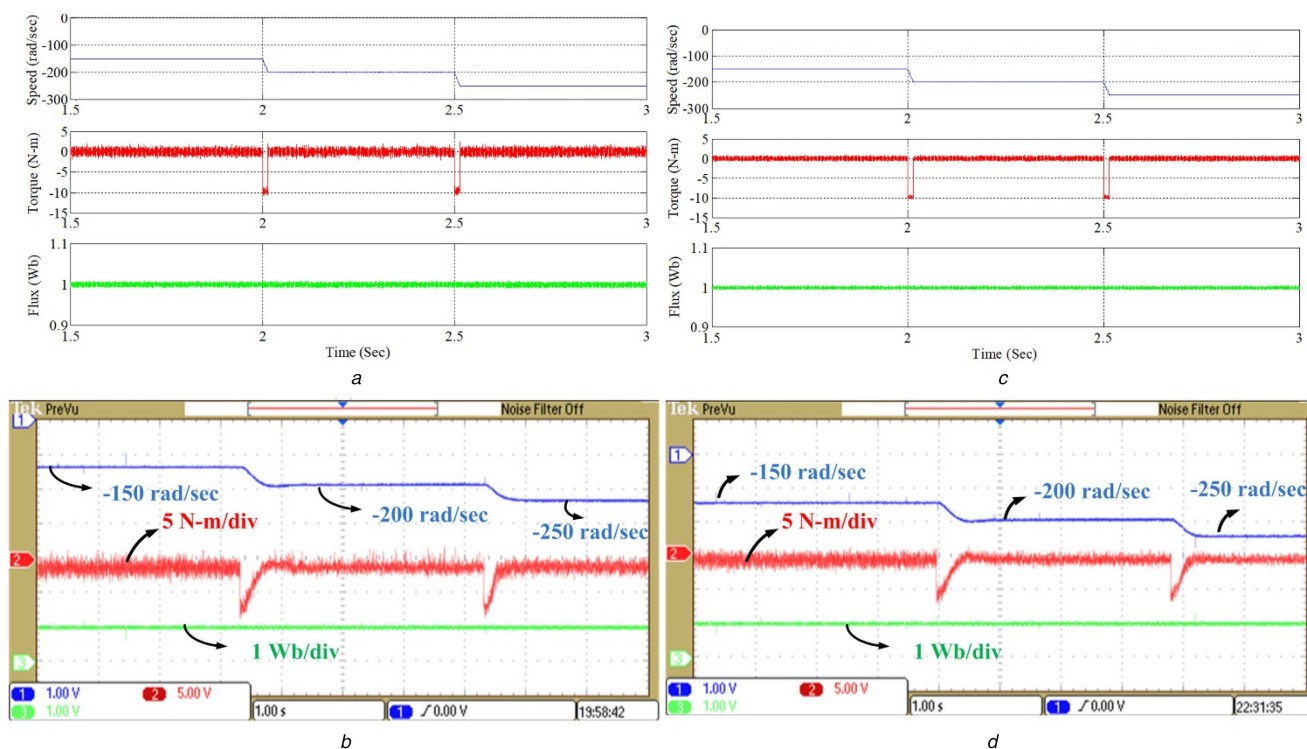
ranking method for dual-inverter fed OEWM drive which relieves PTC from weighting factor assignment. The multiple objectives are considered separately and optimisation is achieved based on minimisation of averaged ranking. The optimised switching states are applied to inverter switches.

To validate the proposed control technique, simulation and experimentation are performed on OEWM drive considering torque, flux ripple and switching frequency limitation objectives. By considering same control objectives, the proposed PTC is compared with the basic PTC. From the obtained results, it can be observed that the proposed scheme exhibits optimal control by minimising torque, flux ripples and switching frequency without weighting factor assignment. Finally, an improvised and effortless control scheme for optimal control of OEWM drive is accomplished.

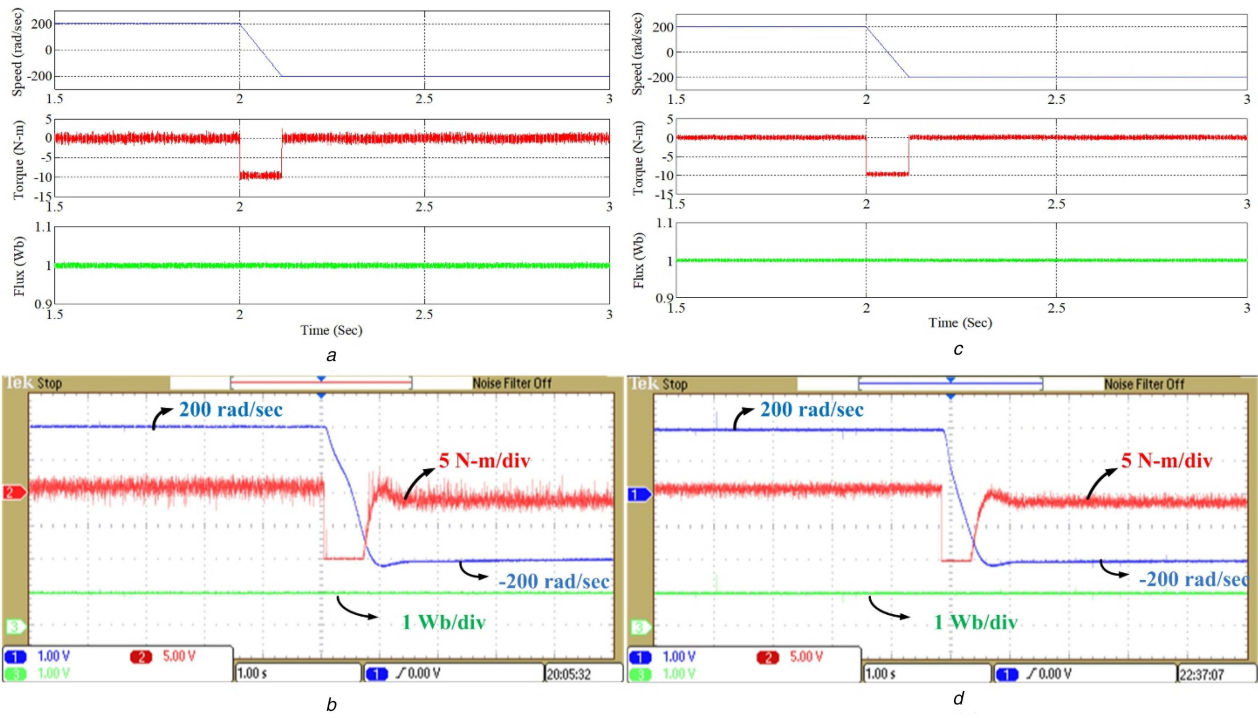




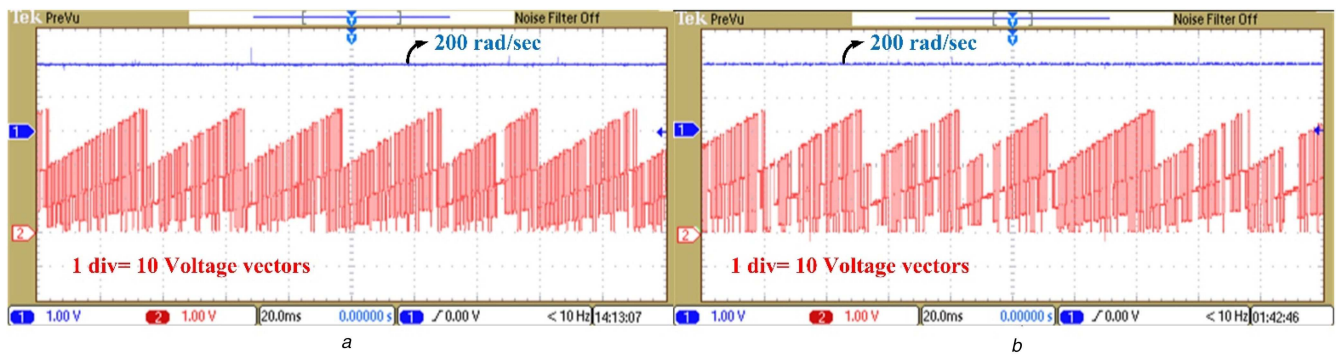
**Fig. 8** Forward motoring speed, torque and flux dynamic characteristics with the step changes in speed from 150 to 200 rad/s and finally 250 rad/s  
(a) Basic PTC simulation, (b) Basic PTC experimental results, (c) Proposed PTC simulation, (d) Proposed PTC experimental results



**Fig. 9** Reverse motoring speed, torque and flux dynamic characteristics with the step changes in speed from -150 to -200 rad/s and finally -250 rad/s  
(a) Basic PTC simulation, (b) Basic PTC experimental results, (c) Proposed PTC simulation, (d) Proposed PTC experimental results



**Fig. 10** Motor speed, torque and flux characteristics during speed reversal operation from +200 to -200 rad/s  
(a) Basic PTC simulation, (b) Basic PTC experimental results, (c) Proposed PTC simulation, (d) Proposed PTC experimental results



**Fig. 11** Switching transitions at 200 rad/s  
(a) Basic PTC response, (b) Proposed PTC response

**Table 4** Experimental analysis of the proposed PTC with existing scheme

Control scheme	Speed, rad/s	Max. torque ripple, N-m	Max. flux ripple, Wb	Avg. switching frequency, Hz
basic PTC	100	4.5	0.04	3018
proposed PTC	100	3	0.031	2524
basic PTC	150	4	0.03	3724
proposed PTC	150	2.8	0.018	3105
basic PTC	250	3	0.02	3458
proposed PTC	250	1.8	0.012	2965

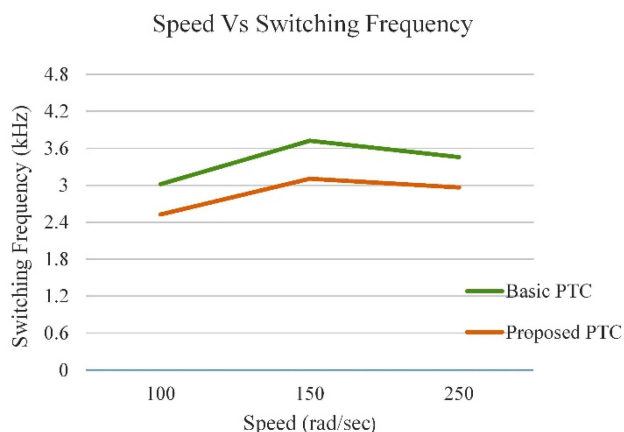


Fig. 12 Switching frequency comparison at different speeds

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