

Some studies on cutting force and temperature in machining Ti-6Al-4V alloy using regression analysis and ANOVA

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ABSTRACT

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The present work deals with the cutting forces and cutting temperature produced during turning of titanium alloy Ti-6Al-4V with PVD TiN coated tungsten carbide inserts under dry environment. The 1st order mathematical models are developed using multiple regression analysis and optimized the process parameters using contour plots. The model presented high determination coefficient ($R^2 = 0.964$ and 0.989 explaining 96.4 % and 98.9 % of the variability in the cutting force and cutting temperature, which indicates the goodness of fit for the model and high significance of the model. The developed mathematical model correlates the relationship of the cutting force and temperature with the process parameters with good degree of approximation. From the contour plots, the optimal parametric combination for lowest cutting force is $v 3$ (75 m/min) – $f 1$ (0.25 mm/rev). Similarly, the optimal parametric combination for minimum temperature is $v 1$ (45 m/min) – $f 1$ (0.25 mm/rev). Cutting speed is found to be the most significance parameter on cutting forces followed by feed. Similarly, for cutting temperature, feed is found to be the most influencing parameter followed by cutting speed.

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1. Introduction

Titanium alloys are extensively used in aerospace, power industries and gas turbine engines. Most of the components of titanium are manufactured by traditional machining techniques such as turning, milling, drilling, reaming and grinding etc. The machinability titanium alloy is poor owing to several inherent properties. Titanium and titanium alloys have low thermal conductivity and high chemical reactivity with many cutting tool materials. Its low thermal conductivity increases the temperature at the cutting edge of the tool. Hence, on machining, the cutting tools wear off very rapidly due to high cutting temperature and strong adhesion between tool and workpiece material. Machining of titanium alloys at higher cutting speed will cause rapid chipping at the cutting edge, which leads to catastrophic failure of the inserts. Therefore proper selections of process parameters are highly essential for effective machining operations.

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Kosaraju et al. (2012) investigated the effect of process parameters on machinability performance characteristics of Titanium using Taguchi Technique. Cutting speed was identified as the most influential process parameter on cutting force and temperature. Davim (2001) studied the influence of cutting conditions on the surface finish in turning using carbide tool based on Taguchi method and established a correlation between cutting parameters with roughness using multiple linear regression analysis. The results indicated that the cutting speed and interaction between cutting speed/feed had a greater influence on surface roughness followed by feed. Depth of cut did not have significance. Dabnun et al. (2005) developed response surface model for surface roughness utilizing factorial DOE and response surface methodology during machinability studies of glass ceramic using uncoated carbide inserts under dry cutting conditions. Feed rate was the main influencing factor on the roughness, followed by the cutting speed and depth of cut. Arbizu and Luis Pérez (2003) developed surface roughness model using RSM. Feed and depth of cut were the factors that influenced the surface roughness.

Singh and Kumar (2006) found that the percent contributions of depth of cut (55.15 %) and feed rate (23.33 %) affecting the feed force was significantly larger as compared to the contribution of the cutting speed (2.63 %) when machining EN24 steel with TiC-coated tungsten carbide inserts using Taguchi's design approach. Sahoo and Sahoo (2012) studied the machinability studies on flank wear, surface roughness, chip morphology and cutting forces in finish hard turning of AISI 4340 steel using uncoated and multilayer TiN and ZrCN coated carbide inserts at higher cutting speed range. The process has also been justified economically for its effective application in hard turning.

Ali MH et al. (2012) presented the prediction of the cost of manufacturing in terms of tool life and machining time saving by using finite-element modeling in machining titanium alloy Ti-6Al-4V. The cutting process of Ti-6Al-4V was simulated using orthogonal cutting finite element model. The work-piece and tool have been designed and presented in a two-dimensional fully thermo-mechanically coupled and define all the parameters into the ABAQUS/EXPLICIT finite-element software. The cemented carbide cutting tool is used for the simulation. Vijay Sekar and Pradeep Kumar (2011) assessed the performance of four material model sets of the Johnson-Cook (JC) constitutive equation in modeling the deformation behavior of Ti6Al4V alloy. The FE code relied on the qualitative nature of inputs such as material flow stress model, friction conditions, fracture criterions and the accuracy of the modeling process. The FE output at steady state conditions was compared with results from orthogonal cutting experiments on a tube of the work material. The effect of the parameters of the JC law and the capabilities of the constitutive equation were analyzed. It was revealed that the used FE model was excellent in predicting the effective stress, strain and temperature, but produced marginal deviations in cutting force and chip morphology predictions. The material model constants computed through an evolutionary computational optimization process and those with conditions similar to machining produced good correlation with experiments.

Ozel and Zeren (2006) presented a methodology to determine flow stress at the machining regimes and friction characteristics at the tool-chip interface from the results of orthogonal cutting tests. This also evaluated several temperature models in calculating the average temperatures at primary and secondary deformation zones and present comparisons with the experimental data obtained for AISI 1045 steel through assessment of machining models (AMM) activity. The proposed methodology was utilized to measured forces and chip thickness obtained through a basic orthogonal cutting test. This conveniently determined the work material flow stress at the primary deformation zone and the interfacial friction characteristics along the tool rake face. This explained a methodology to extend the applicability of a Johnson-Cook work material model to machining regimes. Iqbal et al. (2009) developed the experimental setup and finite element modeling of dry sliding of metals to estimate interface heat transfer coefficient. Heat transfer between the chip, the tool, and the environment during the metal machining process has an impact on temperatures, wear mechanisms and hence on tool-life and on the accuracy of the machined component. For modeling of the metal machining process, the interface heat

transfer coefficient is an important input parameter to quantify the transfer of heat between the chip and the tool and to accurately predict the temperature distribution within the cutting tool. An experimental setup was developed, in which an uncoated cemented carbide pin was rubbed against a steel workpiece while the later was rotated at speeds similar to the cutting tests. A FE model was constructed for heat generation and frictional contact. The experimental and modeling results of the dry sliding process yield the interface heat transfer coefficient for a range of rubbing speeds.

Sun et al. (2009) studied the chip formation during dry turning of Ti6Al4V alloy. It was examined in association with dynamic cutting force measurements under different cutting speeds, feed rates and depths of cut. Both continuous and segmented chip formation processes were observed. The cyclic force frequency increased linearly with cutting speed and decreased inversely with feed rate. The cutting force increased with the feed rate and depth of cut at constant cutting speed due to the large volume of material being removed. The increase in cutting force with increasing cutting speed was attributed to the strain rate hardening at low and high strain rates, respectively. The decrease in cutting force with increasing cutting speed outside these speed ranges was due to the thermal softening of the material.

Iqbal et al. (2008) discussed the effects of the interface heat transfer coefficient on the output of the finite element model of metal cutting process for a wide range of cutting speeds. An updated Lagrangian finite element code DEFORM 2D simulating continuous chip formation was used for the modeling of two dimensional orthogonal machining process. A sensitivity study was performed by varying interface heat transfer coefficient in the simulation of orthogonal cutting process. The effects of varying interface heat transfer coefficient on the simulation output: cutting forces, temperature, shear angle, and chip morphology was analyzed. The simulated results were also compared with the temperature measurement results of high cutting speed experiments. The comparison of simulation results showed that in finite element modeling of the machining process, temperature in tool and chip morphology were significantly influenced by selection of the interface heat transfer coefficient.

Upadhyay et al. (2012) utilized vibration signals for in-process prediction of surface roughness during turning of Ti-6Al-4V alloy. First order and second order multiple regression models using only vibration signals were developed and based on R^2 value and maximum percentage error neither of the two was found to have satisfactory prediction ability. Consequently, Pearson correlation coefficient was used to determine the correlation between surface roughness and cutting parameters and acceleration amplitude of vibrations. Based on Pearson correlation coefficient multiple regression model was developed using above mentioned input parameters. As this model was found accurate enough, neural network model was developed using the same combination of input parameters. Thus, the use of in-process surface roughness prediction can provide an opportunity to take in time corrective action to control the surface finish within required limits.

Sahoo and Sahoo (2012) presented the mathematical modeling and parametric optimization on flank wear and surface roughness based on response surface methodology and grey-based Taguchi method in finish hard turning of AISI 4340 steel using multilayer coated carbide (TiN/TiCN/Al₂O₃/TiN) insert under dry environment. The economical feasibility of utilizing multilayer TiN coated carbide insert was described. Model adequacy was checked using correlation coefficients. Jangra et al. (2011) proved the potential of GRA along with Taguchi method to optimize process parameters for multi-machining characteristics in wire electrical discharge machining of WC-Co composite. Sahoo and Sahoo (2011) developed the mathematical model and parametric optimization for surface roughness in turning D2 steel using TiN coated carbide insert using Taguchi parameter design and response surface methodology. Good correlation between the RSM model predicted values and experimental values exist at 95% confidence intervals and found to be adequate. Kumar et al. (2013) conducted machining of titanium alloys and developed the analytical method to find the convection coefficient and interface

heat transfer coefficients at tool tip-workpiece interface. The experimental and simulated results were compared and validated.

The objectives of present work deals with the study of the effect of cutting speed and feed rate on the components of force and temperature during turning of titanium alloys Ti-6Al-4V using TiN coated carbide inserts under dry environment. The mathematical model and parametric optimization study has also been carried out.

2. Experimental methodology

Experiments have been carried out in dry machining on the MAGNUM MA-1430 lathe. The workpiece material used is Ti6Al4V bar (Grade 5). Ti-6Al-4V offers a combination of high strength, light weight, formability and corrosion resistance which has made it attractive in aerospace applications. The tool material used in the experimental work was PVD TiN coated carbide inserts designated as CNMG120408AP along with the tool holder PCLNR 2020 K12 (Tool geometry: approach angle: 95°, rake angle: -5° and inclination angle: -7°). Experiments have been conducted with cutting speeds (v) of 45, 60, 75 m/min, feed (f) of 0.25, 0.3, 0.35 mm/rev with constant depth of cut of 0.5mm. Nine sets of data have been selected for the experimental tests. Initially, the specimens were turned with 0.5mm cutting depth in order to remove the outer layer. The forces generated during machining i.e. axial force (Fx), radial force (Fy) and tangential force (Fz) were measured by piezoelectric dynamometer (Kistler, 9272). The resultant cutting force (F) was computed. The cutting temperature (T) was measured using infrared temperature measuring equipment (Kiray 300) for every pass at the interface of tool tip and workpiece. The cutting conditions and experimental results are furnished in Table 1 and 2.

Table 1
Cutting conditions

Cutting conditions	Descriptions
Workpiece	Ti6Al4V
Cutting tool	PVD TiN coated carbide
Tool geometry	CNMG120408AP
Tool holder	PCLNR2020K12
Cutting speed, v (m/min)	45, 60, 75
Feed, f (mm/rev)	0.25, 0.3, 0.35
Depth of cut, d (mm)	0.5
Cutting environment	Dry
Responses	Cutting force, cutting temperature

Table 2
Experimental results

No.	v	f	Axial force, Fx (N)	Radial force, Fy (N)	Tangential force, Fz (N)	Resultant cutting force, F (N)	Cutting temperature, T (°C)
1	45	0.25	132	88	445	472	188
2	45	0.3	137	92	453	482	197
3	45	0.35	145	98	479	510	209
4	60	0.25	126	84	426	452	192
5	60	0.3	132	86	442	469	204
6	60	0.35	139	95	463	493	216
7	75	0.25	118	80	395	421	198
8	75	0.3	125	84	414	441	210
9	75	0.35	131	92	425	454	225

3. Results and discussions

3.1 Development of mathematical model

The output dependent variables such as resultant cutting force (F) and cutting temperature (T) can be related as a linear function of independent variables i.e. cutting speed (v) and feed (f). The correlation between them is given by (Thangavel & Selladurai, 2008).

$$F = k_0 + k_1 v + k_2 f, \quad (1)$$

where k_0 is the free term of the regression equation and the coefficients k_1 and k_2 are linear terms respectively. When a multiple linear regression analysis is employed applying least square method, the following equations are obtained in uncoded units as.

$$F = 452.667 - 1.644 v + 373.333 f \quad (R^2 = 96.4\%, R^2(\text{adj}) = 95.2\%) \quad (2)$$

$$T = 106.333 + 0.433 v + 240 f \quad (R^2 = 98.9\%, R^2(\text{adj}) = 98.5\%) \quad (3)$$

The significance test of the regression model and significance on individual model coefficients were performed to verify the goodness of fit for the obtained mathematical model. The analysis of variance (ANOVA) is usually applied to verify the significance of model developed (Singh & Rao, 2007). This analysis is done at a confidence level of 95 % or significance level of 5 % which is shown in Table 3 and Table 4. When the P value for the term is less than 0.05 and calculated F-ratio is more than standard tabulated value, the models are said to be statistically significant. From the ANOVA table, it is revealed that, both the developed models are significant and the terms in the model have the significant effect on the cutting force and temperature.

Table 3
ANOVA table of 1st order model for cutting force (F)

Source	DF	Seq SS	Adj SS	Adj MS	F	P value	Remarks
Regression	2	5741.33	5741.33	2870.67	80.24	0.000	Significant
Residual Error	6	214.67	214.67	35.78			
Total	8	5956					

Table 4
ANOVA table of 1st order model for cutting temperature (T)

Source	DF	Seq SS	Adj SS	Adj MS	F	P value	Remarks
Regression	2	1117.5	1117.5	558.75	268.2	0.000	Significant
Residual Error	6	12.5	12.5	2.083			
Total	8	1130					

Other important coefficient, R^2 , called determination coefficients is also analyzed for the degree of fit. More the value of R^2 (approaches to one), better the mathematical model fits the actual data and residuals are less. The developed mathematical model presented high correlation coefficient ($R^2 = 0.964$ and 0.989) explaining 96.4% and 98.9% of the variability in the cutting force and cutting temperature respectively. It indicates that the model is predicted better for responses. Furthermore, the R^2 and adjusted R^2 values are very close and does not differ so much (Lalwani et al., 2008). It concludes that irrelevant terms are not involved in the model and a good correlation exists between the experimental and predicted values.

Also, from Anderson-Darling test for cutting force and cutting temperature (Fig. 1-2), the data closely follows the straight line and P value is greater than 0.05 at 95 % confidence level. It signifies that the data follow a normal distribution and the model developed by Eq 2-3 is suitable and quite adequate. The residuals fall on a straight line from normal probability plots (Figs. 3-4) suggesting that the errors are distributed normally and the terms mentioned in the model are significant. Also, from **Fig. 5-6** (residuals vs. fitted value), no unusual structure is found. From Fig. 7-8 (residual vs. order of data), it is revealed that the residuals are random in nature and don't exhibit any pattern with run order. Thus, the developed mathematical models can be effectively utilized for prediction of cutting force and cutting temperature in turning.

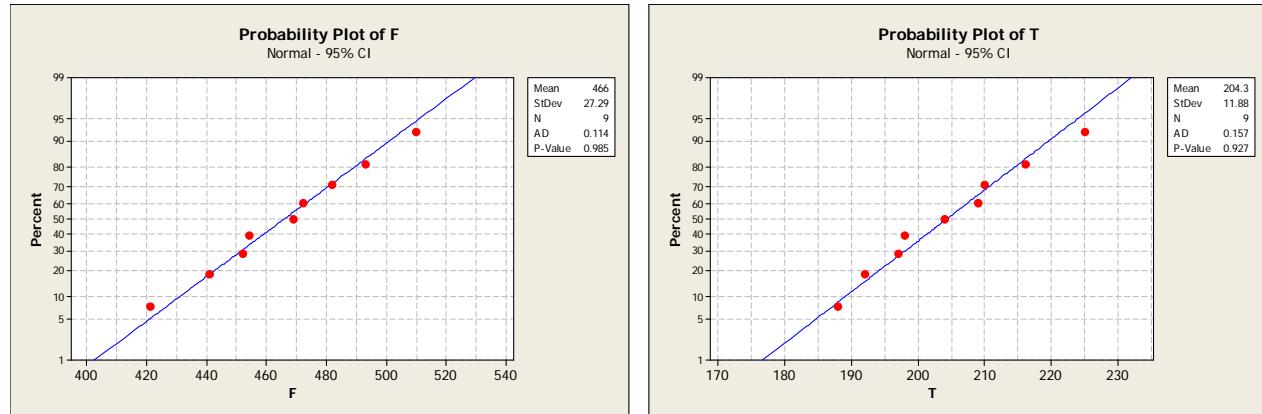


Fig. 1. Anderson Darling test for normality for cutting force (F)

Fig. 2. Anderson Darling test for normality for cutting temperature (T)

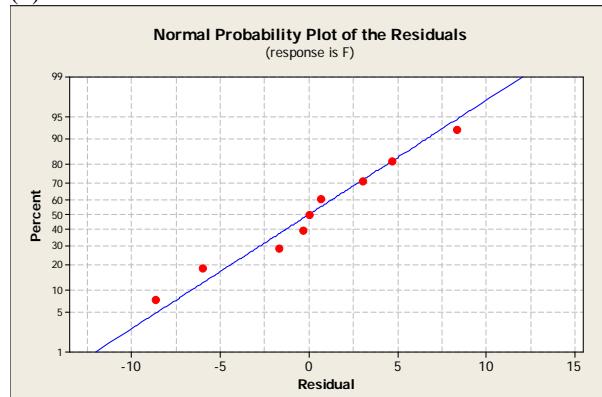


Fig. 3. Normal probability plot of residuals for cutting force (F)

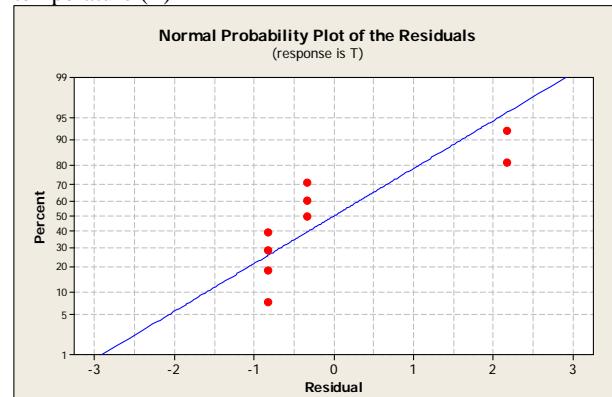


Fig. 4. Normal probability plot of residuals for cutting temperature (T)

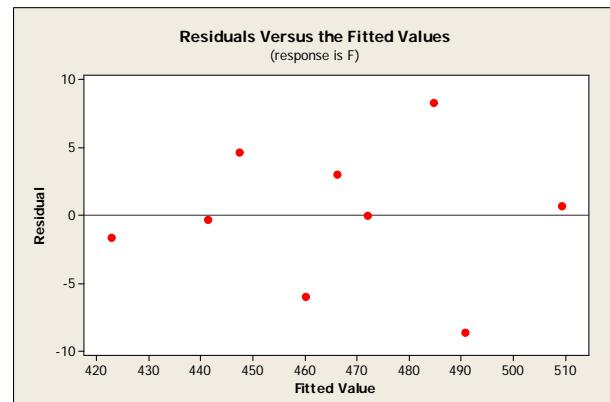


Fig. 5. Residuals vs. fitted values for cutting force (F)

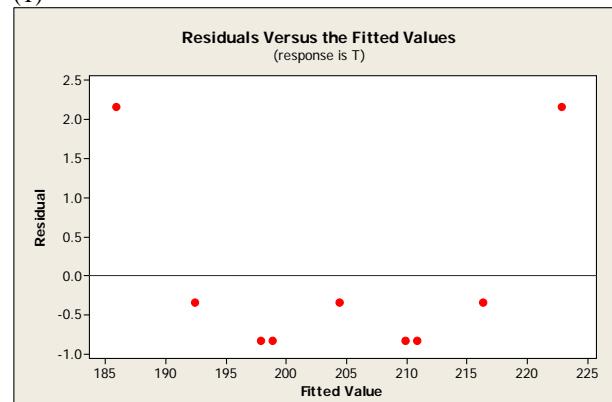


Fig. 6. Residuals vs. fitted values for cutting temperature (T)

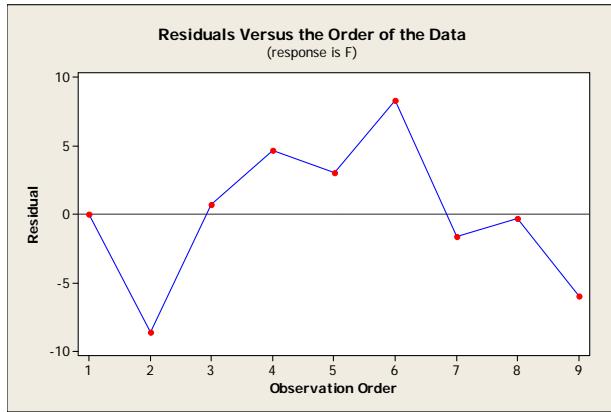


Fig. 7. Residuals vs. order of the data for cutting force (F)

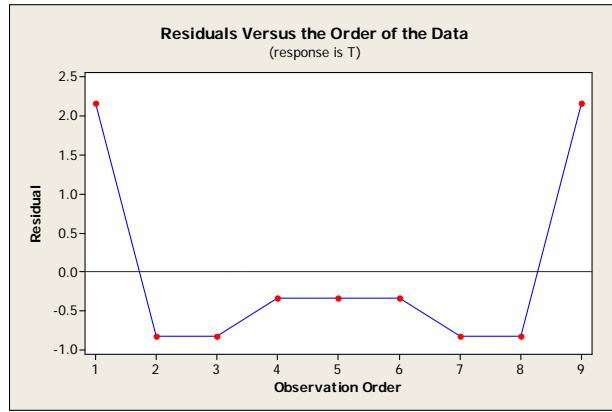


Fig. 8. Residuals vs. order of the data for cutting temperature (T)

For validation of models, some confirmation experiments were conducted using three new sets of process parameters (1c, 2c and 3c) shown in Table 5.

Table 5

Comparison of results obtained from experiment with model

Test	Process parameters		Experiment		Model		Error (%)	
	v	f	F	T	F	T	F	T
1c	50	0.25	468	192	464	188	0.85	2.08
2c	70	0.3	445	206	450	209	-1.12	-1.45
3c	90	0.35	430	238	435	229	-1.16	3.78

Table 5 shows the comparison of cutting force and cutting temperature between the experimental value and model value. The calculated error for cutting force lies between -1.12 to 0.85 % and for cutting temperature, error lies between -1.45 to 3.78 % respectively. Thus, the developed mathematical model can be used to predict the cutting force and cutting temperature within the limits of the factors studied with good degree of approximation.

3.2 Parametric optimization

The optimal parametric combination for both cutting force and temperature are obtained from the study of contour plots (Figs. 9-10). From the cutting speed-feed plane, it is evident that the lower cutting force can be achieved when cutting speed is at highest level (m/min) and feed is at lowest level (mm/rev) and the optimal parametric combination for lowest cutting force is v 3 (75 m/min) – f 1 (0.25 mm/rev). Similarly, the optimal parametric combination for minimum cutting temperature is v 1 (45 m/min) – f 1 (0.25 mm/rev).

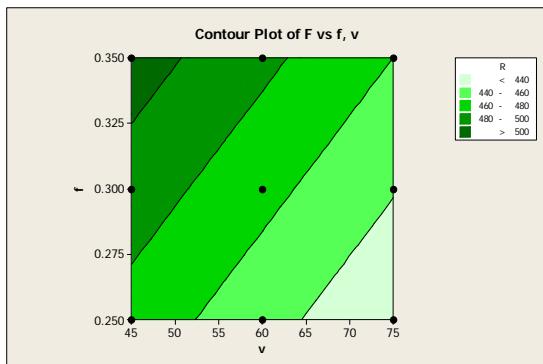


Fig. 9. Contour plot of F vs. v and f

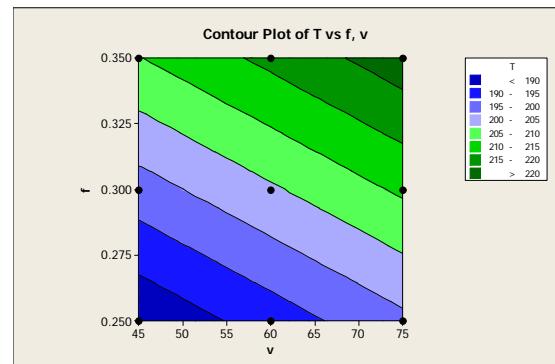


Fig. 10. Contour plot of T vs. v and f

3.3 Effect of process parameters

The effect of process parameters on cutting force and temperature have been studied with the help of main effect plot and analysis of variance. ANOVA analysis tells about the significance of process parameter influencing the responses. The F-test has been carried out at 95 % confidence level. F-value is the ratio of mean square deviations of each parameter to the mean square error. If calculated F-value is greater than F-table value, the parameter is said to be statistically significant. Also if probability of significance (P-value) is less than 0.05 at 95% confidence level, then the factors are said to be statistical significance on responses (Haron et al., 2007).

Table 6 and Table 7 show the results of ANOVA for cutting force and cutting temperature respectively. From Table 6 and Table 7, it is apparent that, the P-values for all the process parameters are less than 0.05 calculated value of F is more than F table value at 95% confidence levels. However, cutting speed is found to be the most significance parameter on cutting forces followed by feed. Similarly, for cutting temperature, feed is found to be the most influencing parameter followed by cutting speed. This trend has also been observed from the main effect plot also (Figs. 11-12). The decreasing trend of cutting force is noticed when the cutting speed is elevated (Fig. 11). At higher cutting speed, cutting temperature is high enough to soften the work material and reduces material shear strength (More et al., 2006). This leads to the evolution of less magnitude of cutting forces at higher cutting speeds during machining titanium alloys.

Table 6
Results of ANOVA for cutting force (F)

Source	DF	Seq SS	Adj SS	Adj MS	F	P	Remarks
v	2	3778.7	3778.7	1889.3	110.06	0.000	Significant
f	2	2108.7	2108.7	1054.3	61.42	0.001	Significant
Error	4	68.7	68.7	17.2			
Total	8	5956					

Table 7
Results of ANOVA for cutting temperature (T)

Source	DF	Seq SS	Adj SS	Adj MS	F	P	Remarks
v	2	254	254	127	50.8	0.001	Significant
f	2	866	866	433	173.2	0.000	Significant
Error	4	10	10	2.5			
Total	8	1130					

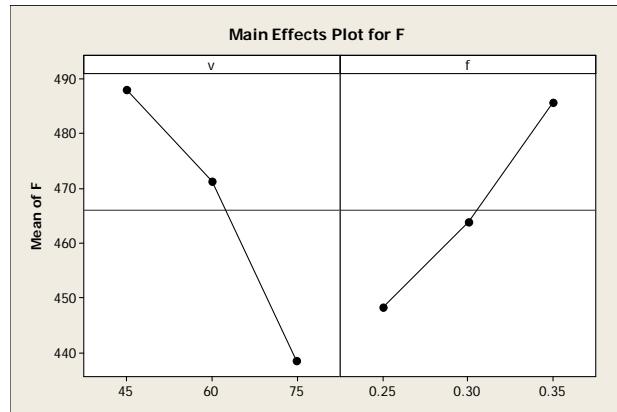


Fig. 11. Main effects plot for cutting force

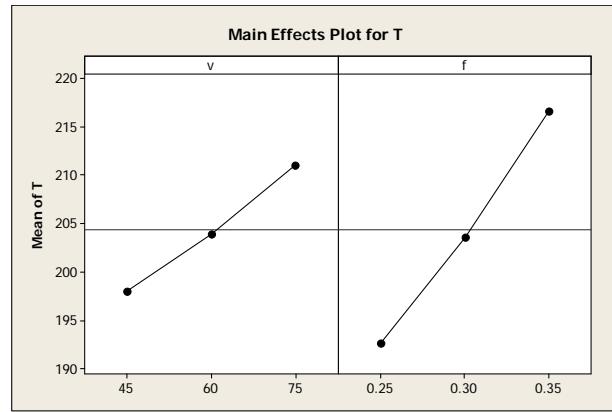


Fig. 12. Main effects plot for cutting temperature

4. Conclusions

The study is based on the experimental investigation, development of mathematical models and parametric optimization in machining titanium alloy using PVD TiN coated carbide insert under dry environment. Therefore based from the findings of the research, following conclusions are drawn:

1. The investigation indicates that the process parameters i.e. cutting speed and feed are the influencing factors which affect the cutting force and temperature in machining. However, cutting speed is found to be the most significance parameter affecting cutting forces whereas feed is for cutting temperature at 95 % confidence level.
2. The mathematical model presented high correlation coefficient ($R^2 = 0.964$ and 0.989) explaining 96.4 % and 98.9 % of the variability in the cutting force and temperature which indicates the goodness of fit for the model and high significance of the model.
3. The data closely follows the straight line observed from Anderson-Darling normality tests. Normal probability plot of models shows that the residuals fall on a straight line implying that errors are distributed normally. It indicates the goodness of fit for the model and high significance of the model.
4. The experimental and predicted values are fairly close to each other. The calculated error for cutting force lies between -1.16-0.85 % and temperature lies between -1.45 - 3.78 percent respectively. The developed equations correlate the relationship of the cutting force and temperature with the process parameters with good degree of approximation and can be effectively utilized for prediction of responses in machining.
5. From the contour plots, the optimal parametric combination for lowest cutting force is found to be cutting speed of 75 m/min and feed of 0.25 mm/rev.
6. From the contour plots, the optimal parametric combination for lowest temperature is found to be cutting speed of 45 m/min and feed of 0.25 mm/rev.

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