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## Crossover temperature ( $T_{CO}$ ) and temperature gradient of refractive indices and length to breadth ratio of 4O.m mesomorphic compounds – an optical study

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Refractive indices as a function of temperature are measured in a number of liquid crystals which belong to the N-(*p*-*n*-butoxy benzylidene)-*p*-*n* alkyl anilines, 4O.m compounds of the famous Schiff's base *n*O.m liquid crystal compounds with  $m = 4$  to 10 and 12. The temperature gradient of refractive indices,  $dn_e/dT$  and  $dn_o/dT$ , of these compounds are estimated. It is well known that in the case of  $dn_o/dT$ , there exists a crossover temperature,  $T_{CO}$ , which exhibits an odd–even effect with the alkyl chain length as expected. Further, using the birefringence data, the length to breadth ratio,  $k$ , for these compounds is estimated, which shows not exactly even–odd effect but irregular change with the chain number. The results are discussed with the body of the data.

**Keywords:** *n*O.m compounds; crossover temperature; birefringence; order parameter

### Introduction

The liquid crystals are one of the important materials which can be used to understand the fundamental laws [1] as well as used in different applications [2]. In order to have technological applications, these materials should possess some interesting physical properties. One of the main properties is that it should possess liquid crystalline nature in and around the room temperature. Further, the birefringence is also an important property in selecting a material for its use in applications and also in the study of the non-linear optics [3,4]. The N-(*p*-*n*-alkoxybenzylidene)-*p*-*n*-alkyl anilines, *n*O.m, form a class of Schiff base compounds, since, they exhibit varying polymorphism with different thermal ranges. The N-(*p*-*n*-butoxybenzylidene)-*p*-*n*-alkyl anilines, 4O.m compounds, exhibit nematic phase with varying thermal ranges (apart from other smectic phases) suitable for the study of birefringence.

In the present article, the temperature gradient of  $n_e$  and  $n_o$  are obtained from the birefringence data taken from literature. Using this data, both  $T_{CO}$  and the length to breadth ratio,  $k$ , are estimated and studied their variation with the alkyl chain number. The results are discussed with the body of the data available in literature. The chemical structure of the molecules is given below.



where  $m = 4$  to 10 and 12

### Simple theory involved in the estimation of $T_{CO}$ and $k$

In order to evaluate the temperature gradients of birefringence and in turn the crossover temperature,  $T_{CO}$ , and the length to breadth ratio,  $k$ , the following parameters such as  $\Delta n$ ,  $\beta$  and  $A$  are needed from the experimental birefringence. Thus, the expressions employed for evaluating these parameters are given below.

de Gennes and Prost [5] pointed out that the anisotropy of any physical quantity can be a measure of orientational order parameter. In the case of uniaxial liquid crystal, this parameter can be defined as

$$Q = \frac{\delta A}{\Delta A} \quad (1)$$

where  $\delta A$  is the anisotropy of any arbitrary physical quantity  $\Delta A = (A_{||} - A_{\perp})$  and  $\Delta A$  is the hypothetical anisotropy of  $A$  in the case of perfect order.

Zywucki and Kuczynski [6] and Kuczynski et al. [7] proposed a simple procedure for the determination of order parameter  $S$  from the birefringence measurements  $\delta n$  without considering the local field experienced by the molecule in a liquid crystal phase. The birefringence  $\delta n$ , which is a function of temperature, is fitted to the following equation:

$$\delta n = \Delta n \left( 1 - \frac{T}{T^*} \right)^{\beta} \quad (2)$$

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where  $T$  is the absolute temperature,  $T^*$  and  $\beta$  are constants ( $T^*$  is about 1–4 K higher than the clearing temperature,  $T_C$  and the exponent  $\beta$  depends on the material but close to 0.20). This procedure enables one to extrapolate  $\delta n$  to the absolute zero temperature.

In practice, the three adjustable parameters  $T^*$ ,  $\Delta n$  and  $\beta$  were obtained by fitting the experimental data for  $\delta n$  to the following equation written in the logarithmic form

$$\log \delta n = \log \Delta n + \beta \log \left( \frac{T^* - T}{T^*} \right) \quad (3)$$

Thus,  $Q$  is given by

$$Q = \frac{\delta n}{\Delta n} \quad (4)$$

Following the procedure of Zywucki and Kuczynski [6] and Kuczynski et al. [7], the authors demonstrated that  $Q$  determined in this way describes well the nematic order parameter and is a good approximation of the order parameter  $S$  given by equation  $S = 1/2 <(3\cos^2\theta - 1)>$ , where  $\theta$  is the angle between the long axis of the molecule and the director ‘ $n$ ’. In general, the order parameter  $S$ , defined by Equation (4), must not necessarily be identical with that defined through other tensorial properties and could be different from the order parameter  $S$  defined by the above equation. However, one can expect that within a given local field model, there should be a relation between macroscopic and microscopic order parameters and following the procedure of Zywucki and Kuczynski [6] and Kuczynski et al. [7], the authors

Table 1. Parameters for (4O.m compounds) the best fit through linear regression for the equation  $\log \delta n = \log \Delta n + \beta \log(T^* - T/T^*)$ .

Compound	$T_C$ (K)	$T^*$ (K)	$\beta$	$\delta n$	
				$\Delta n$	Reg. Coeff.
4O.4	347.40	347.70	0.150	0.390	0.9833
4O.5	354.50	354.51	0.120	0.346	0.9880
4O.6	349.00	349.30	0.130	0.320	0.9575
4O.7	355.80	356.10	0.172	0.362	0.9973
4O.8	351.20	351.50	0.173	0.386	0.9913
4O.9	353.20	353.50	0.142	0.295	0.9962
4O.10	349.70	350.60	0.182	0.310	0.9920
4O.12	350.50	351.90	0.184	0.300	0.9797

also demonstrated it using the example of the Vuks isotropic local field model.

The regression analysis is employed to get the best fit for the three parameters,  $T_C$ ,  $\Delta n$  and  $\beta$  and the values are given in Table 1 for the all compounds studied. The log–log plot to obtain the  $\Delta n$  value is shown in Figure 1 for the compound 4O.7 as a representative case.

Vuks has modified the Lorentz–Lorenz equation for his isotropic model to explain the nematic LC molecule and the following equation expresses the molecular polarisabilities in terms of the experimental refractive indices [8].

$$(n_{e,o}^2 - 1) / (<n^2> + 2) = (4\pi/3)N\alpha_{eo} \quad (5)$$

where  $<n^2> = (n^2_e + 2n^2_o)/3$ .  $N$  is the number of molecules per unit volume.  $\alpha_e$  and  $\alpha_o$  are the molecular polarisabilities. Based on Vuks isotropic model,

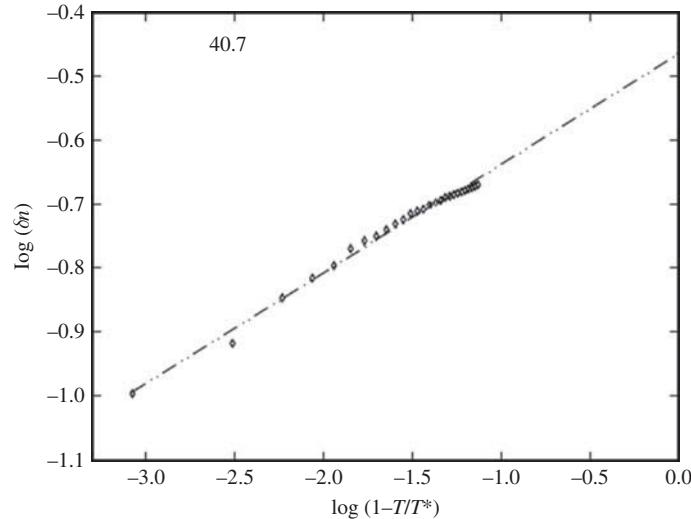


Figure 1. The log–log plot of birefringence  $\delta n$  versus reduced temperature for the 4O.7 compound.

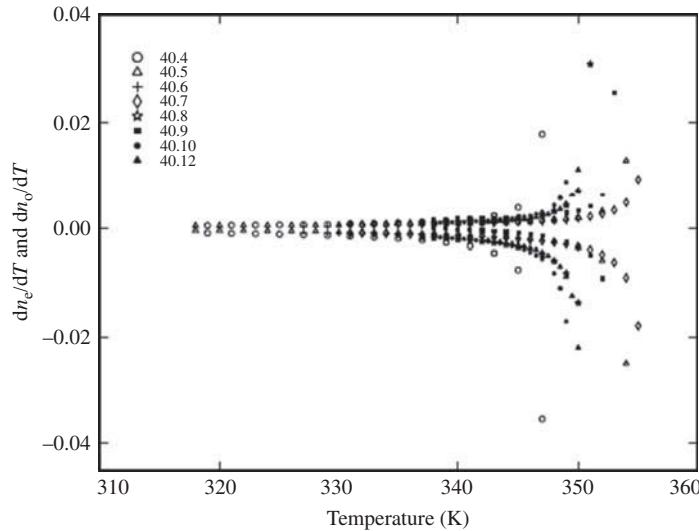


Figure 2. Temperature gradient of refractive indices of 4O.m compounds.

the temperature dependent refractive indices can be written in terms of average refractive index  $\langle n \rangle$  and the birefringence  $\delta n = (n_e - n_o)$  [8]. The refractive indices  $n_e$  and  $n_o$  can be written as

$$n_e = \langle n^2 \rangle^{1/2} + (2/3)(\delta n) \quad (6)$$

and

$$n_o = \langle n^2 \rangle^{1/2} - (1/3)(\delta n) \quad (7)$$

The temperature derivatives of the refractive indices are shown in the following equations:

$$dn_e/dT = (d\langle n \rangle/dT) + (2/3)(d\delta n/dT) \quad (8)$$

$$dn_o/dT = (d\langle n \rangle/dT) + (1/3)(d\delta n/dT) \quad (9)$$

Figure 2 shows the variation of  $dn_e/dT$  and  $dn_o/dT$  with temperature in all the compounds of 4O.m series. In Equation (8), on the right hand side, both the terms are negative and independent of temperature, which implies that  $n_e$  decreases as the temperature increases. However, Equation (9) consists of a negative first term and a positive second term, which is temperature dependent. At low temperatures ( $T < T^*$ ), the second term is less than the first term resulting in a negative  $dn_o/dT$ . With an increase in temperature, the positive term also increases. When  $T \cong T^*$ ,  $dn_o/dT$  jumps to a large positive value. However, in the intermediate stage, there exists a crossover temperature,  $T_{CO}$ , where  $dn_o/dT = 0$ . Further, it is a known fact experimentally [9] that  $\langle n \rangle$  decreases linearly with the

temperature and can be expressed linearly by Equation (10).

From birefringence data, the square of the average refractive index is  $\langle n^2 \rangle = (1/3)(n_e^2 + 2n_o^2)$  and from this we obtain the following:

$$\langle n \rangle = A - BT \quad (10)$$

The crossover temperature is given by the following equation:

$$T_{CO} = T^* \left[ 1 - \left\{ 3BT^*/(\beta\Delta n) \right\}^{1/\beta-1} \right] \quad (11)$$

The refractive index data is taken from literature [10]. Using the above equations, the  $T_{CO}$  in these compounds can be obtained and the values are listed in Table 2 and the variation of  $T_{CO}$  with the alkyl chain number is shown in Figure 3.

In the estimation of the length to breadth ratio,  $k$ , the procedure adopted by Roushdy [11] and the equations of Palffy-Muhoray and Balzarini [12] are used.

Table 2. The intercept and slope values  $A$  and  $B$ , respectively, of 4O.m compounds.

Compound	$A$	$B$	$T_{CO}$ (°C)
40.4	1.7691	-0.000158	-28.4
40.5	1.6157	-0.0003	46.6
40.6	1.5558	-0.000127	-15.8
40.7	1.5296	-0.000293	32.1
40.8	1.9627	-0.0002204	0.4
40.9	1.9502	-0.00022	32.4
40.10	1.7063	-0.000225	15.9
40.12	1.6221	-0.00017	-5.5

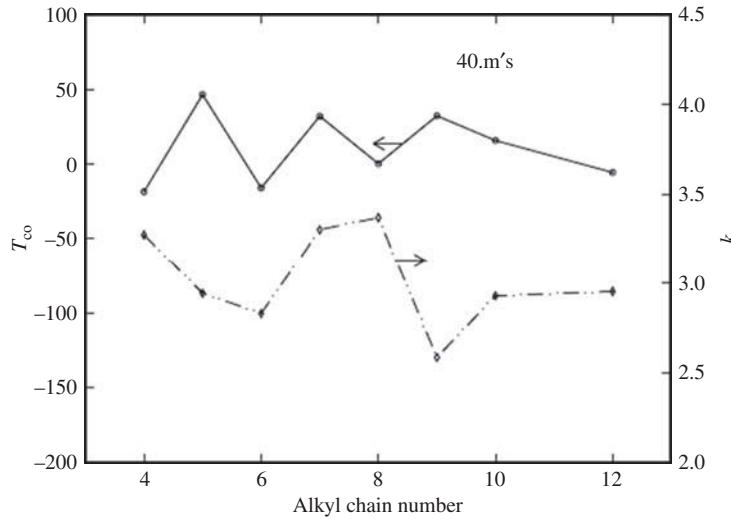


Figure 3. Variation of the crossover temperature,  $T_{CO}$ , and length to breadth ratio,  $k$ , with alkyl chain number.

Palfy-Muhoray and Balzarini [12] have given that the local field  $\eta_{zz}$  for LC molecules is nearly proportional to the order parameter and the slope of that plot is equal to  $[-4(k-1)]/[5(k+2)]$ .  $\eta_{zz}$  is given as follows:

$$\eta_{zz} = (1/3) \left[ \left\{ (n^2 + 2)/(n^2 - 1) (1 + 2dS) \right\} - (n_e^2 + 2)/(n_e^2 - 1) \right] \quad (12)$$

Using the relation given in the text,  $k$ -value is estimated and the values are shown in Figure 3 along with the  $T_{CO}$  value for 4O.m compounds.

## Conclusions

The crossover temperature,  $T_{CO}$ , and the length to breadth ratio,  $k$ , for 4O.m compounds are estimated using the respective equations given in the text. As expected, the  $T_{CO}$  has exhibited an odd–even effect with the alkyl chain number [13]. However, regarding  $k$ , no definite conclusion could be obtained as it has shown neither odd–even effect nor a linear variation. Further, studies on other series of compounds are needed to come to a definite conclusion.

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