

# Estimation of thermodynamic parameters in 3.0m and 30.0m liquid crystalline compounds



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## ARTICLE INFO

### Article history:

Received 7 January 2015

Received in revised form 16 June 2015

Accepted 17 June 2015

Available online 4 July 2015

### Keywords:

Thermo dynamic

Anharmonic and acoustic parameters

Molecular free length

Molecular radius

Bayer's nonlinearity parameter

## ABSTRACT

Thermodynamic parameters such as Moelwyn–Hughes parameter ( $C_1$ ), reduced volume ( $V^*$ ), reduced compressibility ( $\beta$ ), isochoric temperature coefficient of internal pressure ( $X$ ), Sharma parameter ( $S_0$ ), Huggin's parameter ( $F$ ), Grüneisen parameter ( $\Gamma_p$ ), isothermal microscopic Grüneisen parameter ( $\Gamma$ ), fraction free volume ( $f$ ) and acoustical parameters like isothermal ( $K'$ ), isobaric ( $K$ ), isochoric ( $K''$ ) acoustical parameters, isothermal Grüneisen parameter ( $\Gamma_{ith}$ ), isobaric Grüneisen parameter ( $\Gamma_{iba}$ ), isochoric Grüneisen parameter ( $\Gamma_{ich}$ ), reduced Bulk modulus ( $B^*$ ), isothermal Anderson–Grüneisen parameter ( $\delta$ ) and magnitude of repulsive exponent ( $n$ ) are estimated from thermal expansion coefficient,  $\alpha$  obtained from density variation with temperature,  $\rho$  in liquid crystalline N-(p-n-propyl/propyloxybenzylidene)-p-n-alkoxy anilines, 3.0m and 30.0m with  $m = 6, 7$  and  $8$ . In addition to these, the parameters like molecular free length ( $L_f$ ), molecular radius ( $m_r$ ) and nonlinearity parameter, ( $B/A$ ) are also evaluated. The variation of all these parameters are studied both with the temperature in an individual compound and with the chain length in a homologous series. Further, the results agree with the body of the data available.

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## 1. Introduction

Liquid Crystal (LC) materials possessing anisotropic properties are gaining interest of several workers and have been recognized as new dynamic functional molecular materials with wide range of applications in electro-optic display devices. The nature of molecular interactions in LC compounds can be studied from different phase transformations and pretransitional effects [1]. Further, the study of thermo dynamical, anharmonic and acoustical parameters provide information regarding the physico-chemical behavior of the molecules. Moreover, the Bayer's nonlinearity parameter ( $B/A$ ) provides [2] information regarding physical attributes of a material such as internal pressure, intermolecular spacing and acoustic scattering. Thus, the evaluation of these parameters in pure liquids and liquid mixtures has gained much interest from past decade [3–7]. In view of their importance, as a part of our systematic studies, in the present paper we made an attempt to extend the studies to the liquid crystalline compounds N-(p-n-propyl/propyloxybenzylidene)-p-n-alkoxy anilines, 3.0m and 30.0m with  $m = 6, 7$  and  $8$  which exhibit nematic phase with different nematic thermal ranges. The density and refractive index data required for the present compounds is taken from literature [8,9].

## 2. Theory and expressions

The procedure for the estimation of different thermodynamic parameters using the coefficient of thermal expansion ( $\alpha$ ) is taken from literature [10–13] and is given below.

The coefficient of volume expansion is given by ( $\alpha$ ) =  $1/V_m (dV_m/dT)$ , where  $dT = T_2 - T_1$ ,  $dV_m = V_{m2} - V_{m1}$ .

The Moelwyns–Hughes parameter ( $C_1$ ) and reduced molar volume ( $V^*$ ) [3] are evaluated from the following expressions:

$$C_1 = \left(\frac{13}{3}\right) + \left(\frac{1}{\alpha T}\right) + \left(\frac{4\alpha T}{3}\right) \quad (1)$$

$$V^* = \left\{ \frac{\left(\frac{\alpha T}{3}\right)}{(1 + \alpha T)} + 1 \right\}^3 \quad (2)$$

The isochoric temperature coefficient of internal pressure ( $X$ ) is given by

$$X = -\frac{2(1 + 2\alpha T)}{V^{*C_1}} \quad (3)$$

where  $V^{*C_1} = \beta$  is the reduced compressibility.

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Sharma parameter [10–17]  $S_0$  is given by the expression

$$S_0 = \left(-\frac{X}{2}\right)(3 + 4\alpha T). \quad (4)$$

The Huggins parameter [15]  $F$  of a liquid crystal is related to  $S_0$  by the equation

$$F = 2 \left[ 1 + \left( \frac{S_0}{(3 + 4\alpha T)} \right) \right] - \left( 3 + \frac{4\alpha T}{3} \right). \quad (5)$$

Isothermal microscopic Grüneisen parameter ( $\Gamma$ ) is a measure of volume dependence of the harmonicity of the normal mode frequency ( $\nu$ ) of molecular vibrations of a material is related to  $F$  and  $S_0$  as

$$\Gamma = \left(\frac{2}{3}\right) \alpha T + \left(\frac{2 - F + 4\alpha T}{2\alpha T}\right). \quad (6)$$

The fraction free volume ( $f$ ), is a measure of disorder due to increase of mobility of molecules in a liquid crystal and can be expressed in terms of isothermal Grüneisen parameter ( $\Gamma$ ) as

$$f = \frac{1}{(\Gamma + 1)} = \frac{V_a}{V} \quad (7)$$

where  $V_a$  is the available volume. The estimation of  $V_a$  is described below.

Thermal parameter  $A^*$  is a dimensionless parameter which shows that at low temperatures, a liquid crystal tends to be ordered, thereby makes  $A^*$  equal to unity

$$A^* = 1 + \left(\frac{f}{\Gamma}\right). \quad (8)$$

The Grüneisen parameter ( $\Gamma_p$ ) for liquid crystals can be obtained from

$$\Gamma_p = \left(\frac{2}{3}\right) \alpha T + \left(\frac{1}{2\alpha T}\right) + 2. \quad (9)$$

The isochoric acoustical parameter,  $\Delta$  is given as

$$\Delta = \left(\frac{-\alpha T}{2}\right). \quad (10)$$

The reduced Bulk modulus can be given as follows

$$B^* = [V^{-C_1}]^{-1} \quad (11)$$

where  $B^* = B'/B_0$  is the reduced bulk modulus, and  $V^* = V/V_0$  is the reduced volume.  $B'$  and  $V$  is the bulk modulus and volume at temperature  $T$ , and  $B_0'$  and  $V_0$  are the bulk modulus and volume at absolute zero.

The isothermal Anderson–Grüneisen parameter  $\delta$  is known to be an important parameter in the theory of temperature dependence of bulk modulus in solids. It is defined as

$$\delta = 2\Gamma_{iba}. \quad (12)$$

The Anderson–Grüneisen parameter is distinguished from the Moelwyn–Hughes parameter by introducing a new parameter  $\theta$  as

$$\theta = 2(\Gamma_{ith} - \Gamma_{iba}) + 1. \quad (13)$$

The isothermal, isobaric and isochoric Grüneisen parameters are identical to the corresponding acoustical parameters so one can write

$$\Gamma_{ith} = \Gamma_{iba} + \Gamma_{ich}. \quad (14)$$

The isothermal Grüneisen parameter is evaluated using the value of  $C_1$  in Eq. (1). The isochoric Grüneisen parameter  $\Gamma_{ith}$  could be evaluated by using the following equation.

$$\Gamma_{ith} = (C_1 - 1)/2 \quad (15)$$

and

$$\Gamma_{ich} = -(E - F)/F \quad (16)$$

where  $E = [2 + (\alpha T)^{-1}(-2\alpha)(V^{-C_1})]^{-1}$  and  $F = -2\alpha T$ .

Reddy et al. [18–20] demonstrated the following relationship between  $n$ ,  $m$  and  $C_1$  as

$$n = 3C_1 - 12 \quad (17)$$

and

$$m = 3C_1 - (n + 6) \quad (18)$$

where  $m$  and  $n$  are the exponents describing the magnitude of attractive and repulsive force, respectively.

Sharma [21] proposed a theoretical method to establish a relation between the molecular constant  $r$  and isochoric thermo acoustical parameter  $\Delta$  as

$$r = (1 - \Delta)^{-1} = P_i/\varepsilon \quad (19)$$

where  $P_i$  and  $\varepsilon$  is internal pressure and cohesive energy density respectively.

## 2.1. Inter molecular free length ( $L_f$ )

The estimation of  $L_f$  is described below using the thermodynamic parameters. Using the equations (1 to 3), the isothermal ( $K'$ ), isochoric ( $K''$ ) and isobaric ( $K$ ) acoustical parameters are obtained from the following expressions

$$K' = \frac{K}{2} + \frac{K''}{2} \left[ 3 + \frac{(S^* (1 + \alpha T) + X)}{\alpha T} \right] \quad (20)$$

$$K'' = 1 + \left(\frac{X}{2\alpha T}\right) \quad (21)$$

and

$$K = \frac{1}{2} \left[ 1 + \left(\frac{S^* (1 + \alpha T)}{\alpha T}\right) \right] \quad (22)$$

$$\text{where } S^* = 1 + \left(\frac{4\alpha T}{3}\right). \quad (23)$$

The isothermal acoustical parameter ( $K'$ ) is related to the available volume ( $V_a$ ) of the compound as

$$\frac{V_a}{V_m} = \frac{1}{(K' + 1)} = \frac{1}{(K'' + K + 1)} \quad (24)$$

where  $V_m$  is molar volume (molecular weight/density) and the available volume, ( $V_a$ ) can be deduced using the thermo acoustical parameter  $K'$  as

$$V_a = \frac{V_m}{K' + 1}. \quad (25)$$

Then the intermolecular free-length [17] ( $L_f$ ) is given by the relation

$$L_f = \frac{2V_a}{Y} \quad (26)$$

where  $V_a$  represents the available volume per mole and  $Y$  is surface area per mole given by

$$V_{01} = V - V_a \quad (27a)$$

where

$$Y = (36\pi N V_0^2)^{1/3}. \quad (27b)$$

The molar volume at 0 K ( $V_0$ ) can be also obtained by

$$V_{02} = \frac{V}{V^-}. \quad (28)$$

$N$  is the Avogadro number and  $V^-$  is taken from Eq. (2).

Further,  $V_0$  can be obtained directly from molar volume data by extrapolating isotropic data to 0 K.

$B^*$  is another dimensionless parameter and is related to isochoric and isothermal acoustic parameter is given by

$$B^* = [1 + (K - K'')(K' + 1)]^{-1}. \quad (28a)$$

## 2.2. Molecular radius ( $M_r$ )

$M_r$  for the LC molecule can be obtained from density and refractive index results and the relevant expressions are given below [13]

(i) From density,  $\rho$

$$M_r = \frac{1}{2} \sqrt[3]{\frac{M\sqrt{2}}{\rho N}} \quad (29)$$

where  $M$  is the molecular weight.

(ii) The refractive index data can be utilized in conjunction with molar volume to compute the molecular radius ( $M_r$ ) using the following relation [13,14]

$$M_r = \left[ \left( \frac{3}{4\pi N} \right) \frac{(n^2 - 1)}{(n^2 + 2)} V_m \right]^{1/3}. \quad (30)$$

## 2.3. Acoustic nonlinearity parameter, $B/A$

There are a number of reports in literature describing in detail the theoretical and empirical approach for the estimation of  $B/A$  from the thermal expansion coefficient,  $\alpha$  and ultrasonic velocity,  $u$  respectively,

the relevant expressions of the non-linearity parameter,  $B/A$  is given as [22]

$$B/A = 2u\rho[du/dp]_T. \quad (31)$$

General formalism for  $B/A$  in terms of the acoustical parameters for liquids and polymers has been made using Moelwyns–Hughes parameter ( $C_1$ ), isobaric acoustic parameter ( $K$ ) and the isothermal acoustic parameter ( $K''$ ) (the detailed method of calculation of  $K$  and  $K''$  from  $\alpha$  is given elsewhere obtained from the thermal expansion coefficient,  $\alpha$ , and from the ultrasonic velocity,  $u$  respectively). The expressions for  $B/A$  from density are given as

$$B/A = C_1 - 1 \quad (32a)$$

$$B/A = 2K + 2\gamma K''. \quad (32b)$$

## 3. Results and discussion

The thermodynamic parameters such as reduced volume ( $V^-$ ), reduced compressibility ( $\beta$ ), isochoric temperature coefficient of internal pressure ( $X$ ), Sharma parameter ( $S_0$ ), Huggin's parameter ( $F$ ), Grüneisen parameter ( $\Gamma_p$ ), isothermal microscopic Grüneisen parameter ( $\Gamma$ ), fraction free volume ( $f$ ) parameters are evaluated from the coefficient of thermal expansion obtained from density data. The parameter such as Moelwyn–Hughes parameter ( $C_1$ ), is an important parameter to obtain acoustical parameters like isothermal ( $K'$ ), isobaric ( $K$ ), isochoric ( $K''$ ) acoustical parameters, isothermal Grüneisen parameter, ( $\Gamma_{ith}$ ), isobaric Grüneisen parameter, ( $\Gamma_{iba}$ ), isochoric Grüneisen parameter, ( $\Gamma_{ich}$ ), reduced Bulk modulus, ( $B^-$ ), isothermal Anderson–Grüneisen parameter, ( $\delta$ ) and magnitude of repulsive exponent, ( $n$ ). It is already known that  $C_1$  offers the simplest scale for the determination of molecular ordering, structure, interactions and anharmonicity in some materials [12]. In addition to these, the parameters like molecular free length ( $L_f$ ), molecular radius ( $M_r$ ) and nonlinearity parameter, ( $B/A$ ) are also evaluated. The results are compared with those obtained for similar nature of compounds viz., nO.Om compounds. Recently, extensive studies are reported regarding the estimation of the thermodynamic parameters for a number of nO.m liquid crystalline compounds utilizing the available dilatometric, ultrasonic velocity and birefringence data [13]. The data pertinent to the above parameters for all the compounds are presented in Tables 1 to 5 and their variation with temperature and chain length is given in Figs. 1 to 6.

The salient features observed from the study are

1. All the parameters exhibit a constant value in a particular phase except in the vicinity of phase transition where they exhibit singularity, (Figs. 1 to 4).

**Table 1**  
Variation of anharmonic parameters such as Moelwyn–Hughes parameter ( $C_1$ ), reduced volume ( $V^-$ ), reduced compressibility ( $\beta$ ), isochoric temperature coefficient of internal pressure ( $X$ ), Sharma parameter ( $S_0$ ), Huggin's parameter ( $F$ ), fraction free volume ( $f$ ) in isotropic and nematic LC of all the compounds.

| Comp. | Temp. | Phase | $V^-$ | $C_1$ | $\beta = V^{-C_1}$ | $X_1$ | $X$   | $S_0$ | $F$  | $\Gamma$ | $f$  | $A^*$ |
|-------|-------|-------|-------|-------|--------------------|-------|-------|-------|------|----------|------|-------|
| 3.06  | 83.9  | Iso   | 1.12  | 11.93 | 4.02               | −1.27 | −0.63 | 1.12  | 1.45 | 4.12     | 0.20 | 1.05  |
|       | 68.0  | N     | 1.24  | 8.17  | 5.87               | −1.58 | −0.54 | 1.12  | 1.15 | 3.66     | 0.21 | 1.06  |
| 3.07  | 81.0  | Iso   | 1.13  | 11.63 | 4.08               | −1.28 | −0.63 | 1.12  | 1.44 | 4.08     | 0.20 | 1.05  |
|       | 68.0  | N     | 1.25  | 8.09  | 5.97               | −1.59 | −0.53 | 1.12  | 1.14 | 3.65     | 0.22 | 1.06  |
| 3.08  | 83.1  | Iso   | 1.14  | 11.22 | 4.17               | −1.30 | −0.62 | 1.12  | 1.42 | 4.03     | 0.20 | 1.05  |
|       | 70.0  | N     | 1.25  | 7.99  | 6.12               | −1.62 | −0.53 | 1.12  | 1.12 | 3.64     | 0.22 | 1.06  |
| 30.06 | 114   | Iso   | 1.24  | 8.13  | 5.92               | −1.59 | −0.54 | 1.12  | 1.14 | 3.65     | 0.21 | 1.06  |
|       | 98.5  | N     | 1.28  | 7.68  | 6.66               | −1.69 | −0.51 | 1.11  | 1.05 | 3.61     | 0.22 | 1.06  |
| 30.07 | 111   | Iso   | 1.26  | 7.89  | 6.28               | −1.64 | −0.52 | 1.12  | 1.10 | 3.63     | 0.22 | 1.06  |
|       | 97.0  | N     | 1.30  | 7.51  | 7.06               | −1.75 | −0.49 | 1.11  | 1.00 | 3.59     | 0.22 | 1.06  |
| 30.08 | 109   | Iso   | 1.26  | 7.90  | 6.25               | −1.64 | −0.52 | 1.12  | 1.10 | 3.63     | 0.22 | 1.06  |
|       | 96.5  | N     | 1.30  | 7.50  | 7.08               | −1.75 | −0.49 | 1.11  | 1.00 | 3.59     | 0.22 | 1.06  |

**Table 2**

Variation of parameters such as isothermal ( $K'$ ), isochoric ( $K''$ ) and isobaric ( $K$ ) acoustical parameters, available volume ( $V_a$ ) and molecular free length ( $L_f$ ) in isotropic and nematic LC phases of all the compounds.

| Comp  | Temp °C | Phase | $k''$  | $k$   | $k'$  | $V_a$  | $V_{01}$ | $V_{02}$ | $L_{f1}$ | $L_{f2}$ |
|-------|---------|-------|--------|-------|-------|--------|----------|----------|----------|----------|
| 3.06  | 83.9    | Iso   | −1.357 | 8.670 | 7.314 | 40.624 | 297.114  | 300.579  | 0.447    | 0.434    |
|       | 68.0    | N     | 0.053  | 4.808 | 4.861 | 56.771 | 275.986  | 267.907  | 0.656    | 0.669    |
| 3.07  | 81.0    | Iso   | −1.246 | 8.367 | 7.121 | 43.531 | 309.990  | 313.265  | 0.466    | 0.462    |
|       | 68.0    | N     | 0.082  | 4.728 | 4.810 | 59.978 | 288.515  | 279.431  | 0.673    | 0.687    |
| 3.08  | 83.1    | Iso   | −1.095 | 7.955 | 6.860 | 47.045 | 322.717  | 325.557  | 0.49     | 0.487    |
|       | 70.0    | N     | 0.124  | 4.615 | 4.739 | 63.634 | 301.545  | 291.049  | 0.693    | 0.71     |
| 30.06 | 113.5   | Iso   | 0.067  | 4.771 | 4.838 | 60.402 | 292.197  | 283.345  | 0.672    | 0.686    |
|       | 98.5    | N     | 0.245  | 4.285 | 4.530 | 62.724 | 284.147  | 271.014  | 0.711    | 0.734    |
| 30.07 | 111     | Iso   | 0.159  | 4.518 | 4.677 | 65.322 | 305.525  | 293.950  | 0.705    | 0.724    |
|       | 97.0    | N     | 0.316  | 4.094 | 4.409 | 67.560 | 297.879  | 281.696  | 0.742    | 0.77     |
| 30.08 | 109     | Iso   | 0.156  | 4.527 | 4.683 | 67.669 | 316.876  | 304.962  | 0.713    | 0.732    |
|       | 96.5    | N     | 0.318  | 4.086 | 4.405 | 70.052 | 308.554  | 291.692  | 0.751    | 0.78     |

**Table 3**

Variation of parameters such as Grüneisen parameter ( $\Gamma_p$ ), isothermal microscopic Grüneisen parameter ( $\Gamma$ ), isothermal Anderson–Grüneisen parameter ( $\delta$ ), Anderson–Grüneisen parameter ( $\theta$ ), exponents describing the magnitude of attractive and repulsive force  $m$  and  $n$  in isotropic and nematic LC phase of all the compounds.

| Comp. | Temp. | Phase | $\Gamma$ | $\Gamma_p$ | $\Delta$ | $B^-$ | $E$  | $F$   | $\Gamma_{ith}$ | $\Gamma_{ich}$ | $\Gamma_{iba}$ | $\delta$ | $\theta$ | $\theta^*$ | $r$  | $m$  |
|-------|-------|-------|----------|------------|----------|-------|------|-------|----------------|----------------|----------------|----------|----------|------------|------|------|
| 3.06  | 83.9  | Iso   | 4.12     | 5.80       | 112.85   | 0.25  | 0.51 | −0.27 | 5.46           | 2.87           | 2.59           | 5.17     | 6.75     | 5.17       | 2.72 | 6.00 |
|       | 68    | N     | 3.66     | 3.92       | 91.71    | 0.17  | 0.51 | −0.58 | 3.58           | 1.88           | 1.71           | 3.41     | 4.75     | 3.41       | 2.17 | 6.00 |
| 3.07  | 81    | Iso   | 4.08     | 5.65       | 111.23   | 0.25  | 0.51 | −0.28 | 5.31           | 2.80           | 2.51           | 5.03     | 6.59     | 5.03       | 2.69 | 6.00 |
|       | 68    | N     | 3.65     | 3.88       | 91.03    | 0.17  | 0.51 | −0.59 | 3.54           | 1.86           | 1.69           | 3.38     | 4.71     | 3.38       | 2.15 | 6.00 |
| 3.08  | 83.1  | Iso   | 4.03     | 5.44       | 110.84   | 0.24  | 0.51 | −0.30 | 5.11           | 2.69           | 2.42           | 4.83     | 6.38     | 4.83       | 2.65 | 6.00 |
|       | 70    | N     | 3.64     | 3.83       | 90.55    | 0.16  | 0.51 | −0.62 | 3.49           | 1.83           | 1.67           | 3.33     | 4.65     | 3.33       | 2.12 | 6.00 |
| 30.06 | 113.5 | Iso   | 3.65     | 3.90       | 103.59   | 0.17  | 0.51 | −0.59 | 3.56           | 1.87           | 1.70           | 3.40     | 4.73     | 3.40       | 2.16 | 6.00 |
|       | 98.5  | N     | 3.61     | 3.68       | 94.44    | 0.15  | 0.51 | −0.69 | 3.34           | 1.74           | 1.60           | 3.21     | 4.47     | 3.21       | 2.04 | 6.00 |
| 30.07 | 111   | Iso   | 3.63     | 3.78       | 100.34   | 0.16  | 0.51 | −0.64 | 3.45           | 1.80           | 1.65           | 3.30     | 4.60     | 3.30       | 2.10 | 6.00 |
|       | 97    | N     | 3.59     | 3.59       | 91.55    | 0.14  | 0.51 | −0.75 | 3.25           | 1.68           | 1.57           | 3.14     | 4.36     | 3.14       | 1.98 | 6.00 |
| 30.08 | 109   | Iso   | 3.63     | 3.79       | 99.91    | 0.16  | 0.51 | −0.64 | 3.45           | 1.80           | 1.65           | 3.30     | 4.60     | 3.30       | 2.10 | 6.00 |
|       | 96.5  | N     | 3.59     | 3.58       | 91.33    | 0.14  | 0.51 | −0.75 | 3.25           | 1.68           | 1.57           | 3.14     | 4.36     | 3.14       | 1.98 | 6.00 |

- From the data, it is observed that if coefficient of volume expansion is low its  $C_1$  value is high. From Table 1 it is known that  $C_1$  is low in nematic phase and high in isotropic phase. The parameters reduced volume,  $V^-$ , reduced compressibility,  $V^{-C_1}$ , and the isochoric temperature coefficient of internal pressure, ( $X$ ) and their variation with temperature is similar to that of thermal expansion coefficient  $\alpha$ , as expected and in all compounds as these parameters are proportional to  $\alpha$ . The variation of reduced volume  $V^-$  and  $C_1$  with the temperature in 30.06 is shown in Fig. 1.
- From Table 1 it is observed that the parameters  $C_1$ ,  $X'$ ,  $F$ ,  $\Gamma$ ,  $\Delta$ ,  $\Gamma_p$  are exhibiting low values in liquid crystalline phases compared to the isotropic phase which shows the molecular ordering increases as the temperature decreases in liquid crystal phases.
- From Fig. 2 it is known that the Sharma parameter,  $S_0$  is constant around  $1.13 \pm 0.05$  irrespective of the nature and state of the compound including the liquid crystals.  $S_0$  tends to be independent of the value of  $\alpha$  for any material. However, at and in the immediate vicinity of the liquid crystalline phase transformations the value of  $S_0$

abruptly falls to a minimum as the parameter  $S_0$  [20] is indirectly proportional to  $\alpha$ .

- The fractional free volume ( $f$ ) which determines the disorder due to the mobility of molecules in the compound. Hence, the relations viz.,  $S_0 = 5.5 * f$  and  $A^* = 5.25 * f$  hold good in these compounds also as in the case of other nO.m compounds [14].
- It is observed that the available volume,  $V_a$  is more in liquid crystalline phase than in isotropic phase and its variation with temperature for the case of all the compounds is given in Table 2 and Fig. 5. From the Figure it is known that  $V_a$  is more in 30.0m compounds than in 3.0m compounds.
- The isothermal Anderson–Grüneisen parameter  $\delta$  is known to be an important parameter in the theory of temperature dependence of bulk modulus in solids [23]. Fig. 3 depicts its variation with temperature in 3.06 compound. From Table 3 the magnitude of  $m$  is recognized as 6 in the case of liquid crystalline compounds which is in agreement with the literature [23].

**Table 4**

Variation of non linearity parameter,  $B/A$  in isotropic and nematic LC phase of all the compounds.

| Comp. | Temp. | Phase | $B/A$ (K) | $B/A$ ( $C_1$ ) |
|-------|-------|-------|-----------|-----------------|
| 3.06  | 83.9  | Iso   | 8.238     | 10.924          |
|       | 68    | N     | 7.313     | 7.167           |
| 3.07  | 81    | Iso   | 8.161     | 10.624          |
|       | 68    | N     | 7.297     | 7.092           |
| 3.08  | 83.1  | Iso   | 8.057     | 10.219          |
|       | 70    | N     | 7.275     | 6.986           |
| 30.06 | 113.5 | Iso   | 7.306     | 7.132           |
|       | 98.5  | N     | 7.215     | 6.683           |
| 30.07 | 111   | Iso   | 7.256     | 6.896           |
|       | 97    | N     | 7.184     | 6.508           |
| 30.08 | 109   | Iso   | 7.258     | 6.904           |
|       | 96.5  | N     | 7.183     | 6.502           |

**Table 5**

Variation of molecular radius,  $M_r$  obtained from Eqs. (29) and (30) in isotropic and nematic LC phase of all the compounds.

| Comp. | Temp. | Phase | $M_r$ (density) | $M_r$ optics |
|-------|-------|-------|-----------------|--------------|
| 3.06  | 83.9  | Iso   | 4.638           | 3.476        |
|       | 68    | N     | 4.605           | 3.557        |
| 3.07  | 81    | Iso   | 4.699           | 3.540        |
|       | 68    | N     | 4.676           | 3.600        |
| 3.08  | 83.1  | Iso   | 4.770           | 3.581        |
|       | 70    | N     | 4.750           | 3.681        |
| 30.06 | 113.5 | Iso   | 4.700           | 3.570        |
|       | 98.5  | N     | 4.720           | 3.651        |
| 30.07 | 111   | Iso   | 4.773           | 3.600        |
|       | 97    | N     | 4.751           | 3.691        |
| 30.08 | 109   | Iso   | 4.832           | 3.599        |
|       | 96.5  | N     | 4.807           | 3.699        |

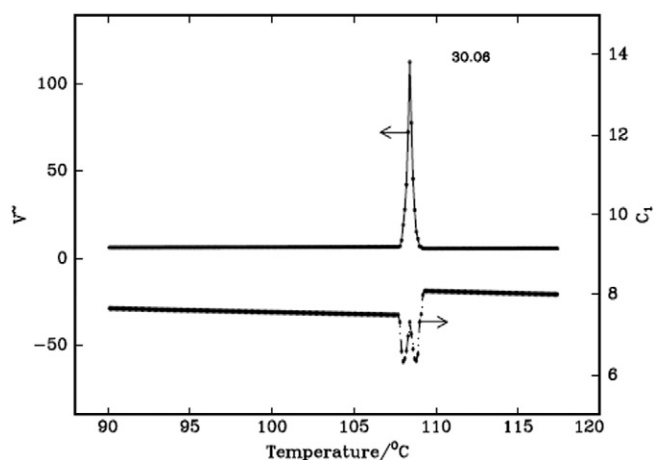


Fig. 1. Variation of reduced volume ( $V_r$ ) and Moelwyn-Hughes parameter ( $C_1$ ) with temperature in 30.06 compound.

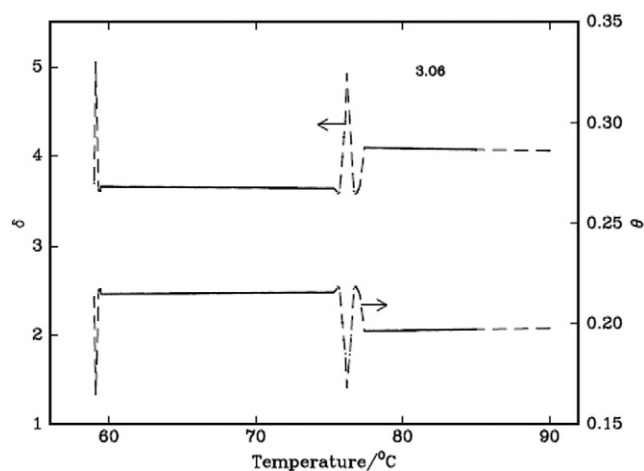


Fig. 3. Variation of isothermal Anderson-Grüneisen parameter ( $\delta$ ) and Anderson Gruneisen parameter ( $\theta$ ) with temperature in 3.06 compound.

8. The isothermal Grüneisen parameter  $\Gamma_{ith}$  is a measure of anharmonicity of molecular vibration, the isothermal, isochoric, isobaric Grüneisen parameters also show the consistent values in any particular phase but decreases slightly in LC phases from isotropic phase. The values of  $\Gamma_{ith}$ ,  $\Gamma_{iba}$ ,  $\Gamma_{ich}$  are given in Table 3 for the all the present studied compounds. The variation of  $\Gamma_{ith}$ ,  $\Gamma_{iba}$ ,  $\Gamma_{ich}$  with temperature is shown for the compound 3.08 in Fig. 4. The parameter  $\Gamma_{iba}$  exhibits almost a similar trend as  $\Gamma_{ith}$  and  $\Gamma_{iba}$  is less than  $\Gamma_{ith}$ .
9. The molecular free length ( $L_f$ ) are calculated from available volume  $V_a$  and molar volume ( $V_o$ ). However,  $V_o$  can be evaluated using different expressions. The  $V_o$  is estimated in two ways and the values at different temperatures in LC phases given in Table 2 reveal that  $V_o$  values show agreement with one another. It has been reported earlier, from the systematic studies on the benzoic acids as well as in a number of nO.m compounds [13] found that the slope value should be around  $8 \times 10^{-4}$  to obtain reasonable agreement. The molecular free length values in all the compounds in both the series are of comparable magnitude and the isotropic values are slightly lower compared to LC phases. The variation of  $L_f$  with temperature is depicted in Fig. 6 for the case of all compounds.
10. The data from Table 4 reveals that the  $B/A$  value almost remains constant in a particular phase except in the vicinity of the phase transition where it shows a peak and the peak magnitude depends on  $\alpha$ , and further, the magnitude of  $B/A$  is slightly smaller in LC phases compared to that in isotropic phase.

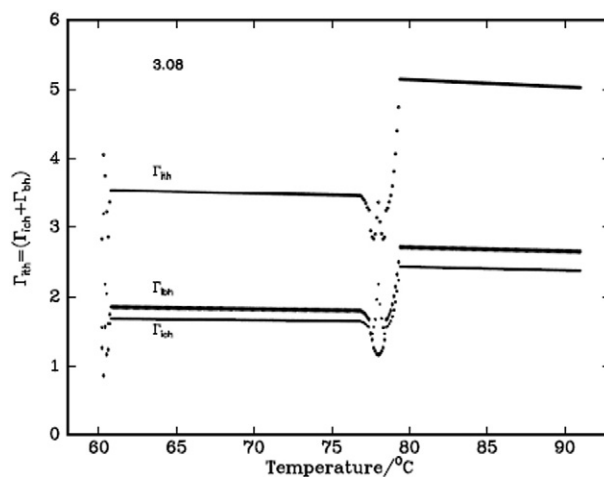


Fig. 4. Variation of isothermal Gruneisan parameter  $\Gamma_{ith} = \Gamma_{iba} + \Gamma_{ich}$  with temperature in 3.08 compound.

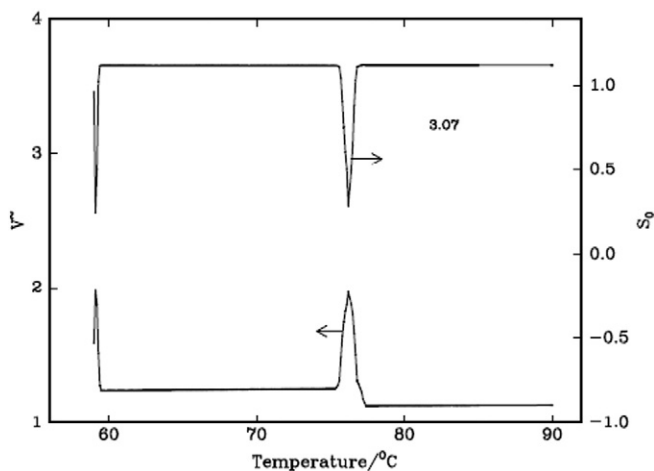


Fig. 2. Variation of reduced volume ( $V_r$ ) and Sharma parameter ( $S_0$ ) with temperature in 3.07 compound.

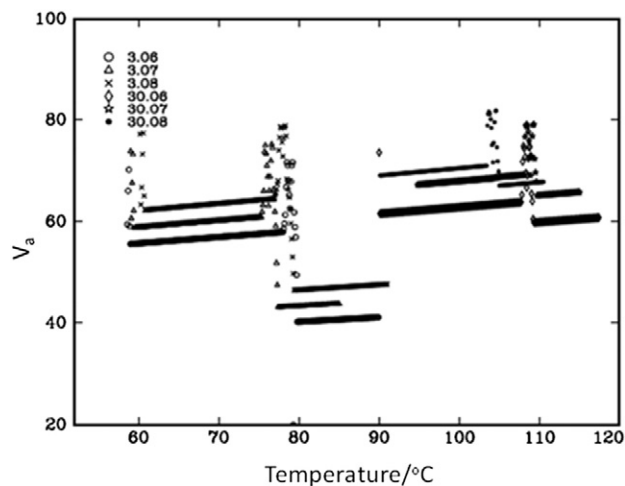
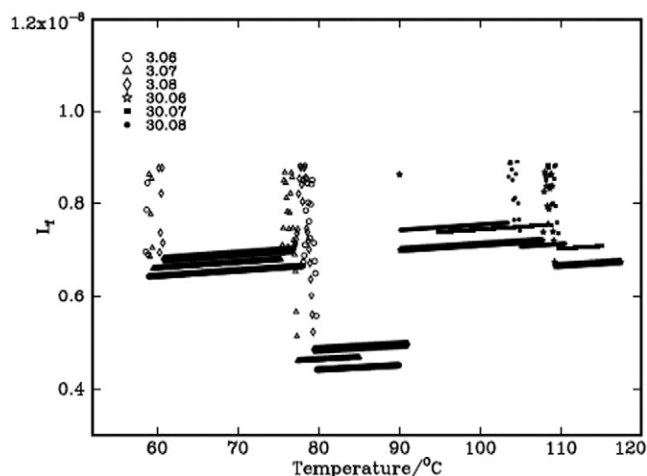


Fig. 5. Variation of available volume ( $V_a$ ) with temperature in 3.0m and 30.0m compounds.



**Fig. 6.** Variation of Molecular free length ( $L_f$ ) with temperature in 3.0m and 30.0m compounds.

11. Generally this parameter,  $B/A$  lies in the range 5.5 to 9.5, with extreme variations of 2 and 13. These extreme values are reported in some cases [24] and
12. The molecular radius,  $M_r$ , estimated from birefringence is low compared to that obtained from  $\alpha$ . Further, it is found from the Table 5 the increment of molecular radius for methylene unit is found to be 0.066 Å from density and 0.053 Å from birefringence and 0.066 Å from density and 0.057 Å from birefringence in 3.0m and 30.0m materials respectively.

#### Acknowledgments

The authors Dr. P. Pardha Saradhi and Dr. V. G. K. M. Pisipati express their thanks to the head, ECE Department and the Management of K.L. University, Vaddeswaram 522 502, India for providing the facilities.

One of the authors P.V. Datta Prasad acknowledges the S.S.D. Polymers for providing some facilities during the work. This work is supported by the Department of Science and Technology (Grant No: SR/S2/CMP-0071/2008). D. Madhavi Latha acknowledges the financial support of DST-WOS-A through grant no. SR/WOS-A/PS-05/2010.

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